

# Automata Learning for Dynamic Software Product Lines

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# Acknowledgments

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The material presented in the slides are due to many researchers, explicitly acknowledged at the respective slides.

My research has been partially funded by:  
**UKRI TAS Node on Verifiability** and **EPSRC VSL-Q Grants.**





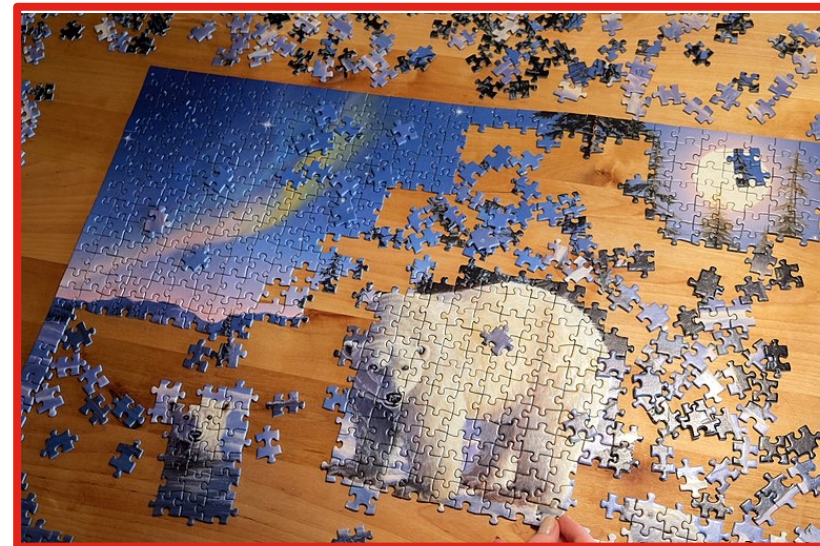
**Active Automata Learning**



**Adaptive Learning**



**Product-Line Learning**



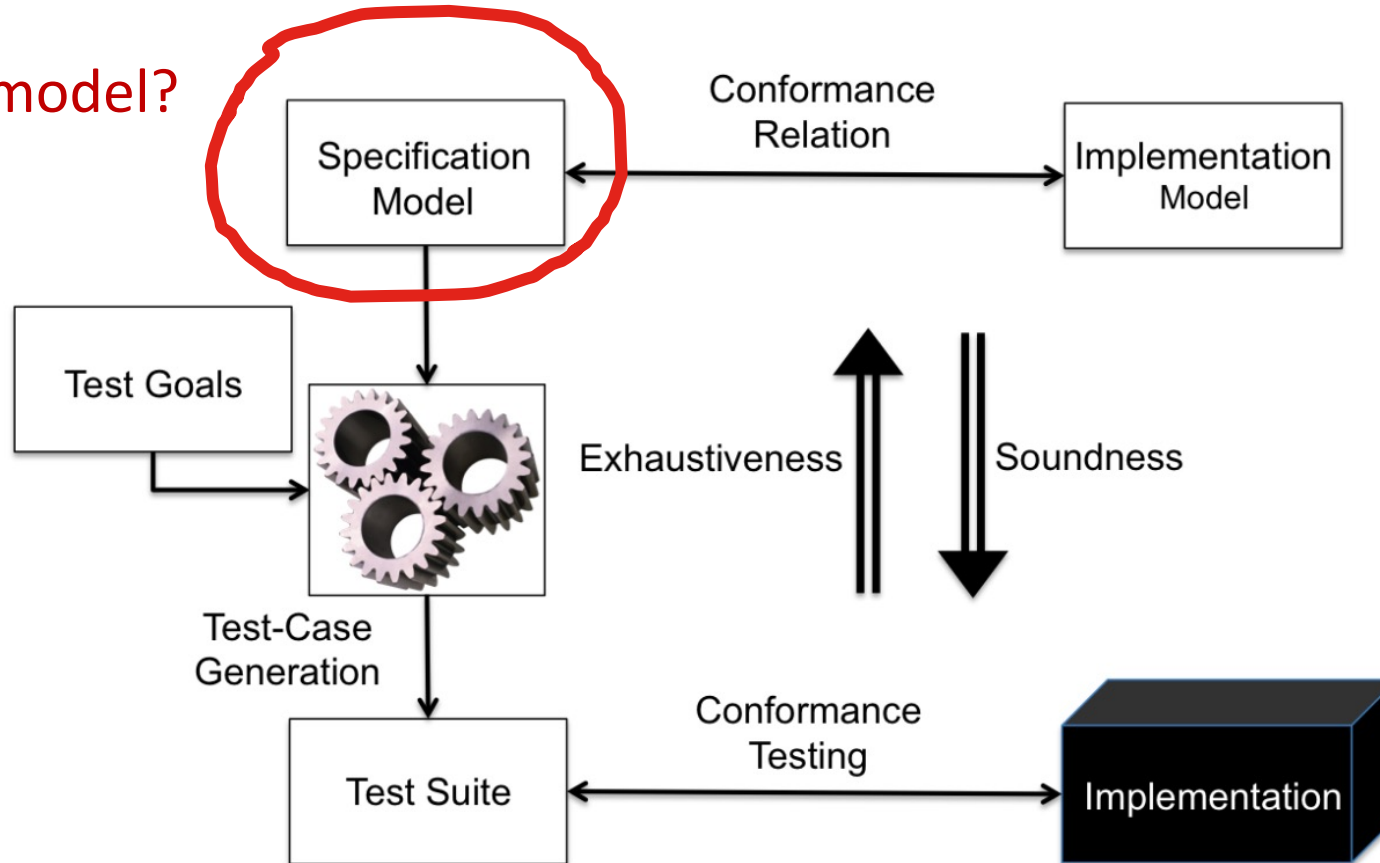
**Compositional Learning**

# Active Automata Learning

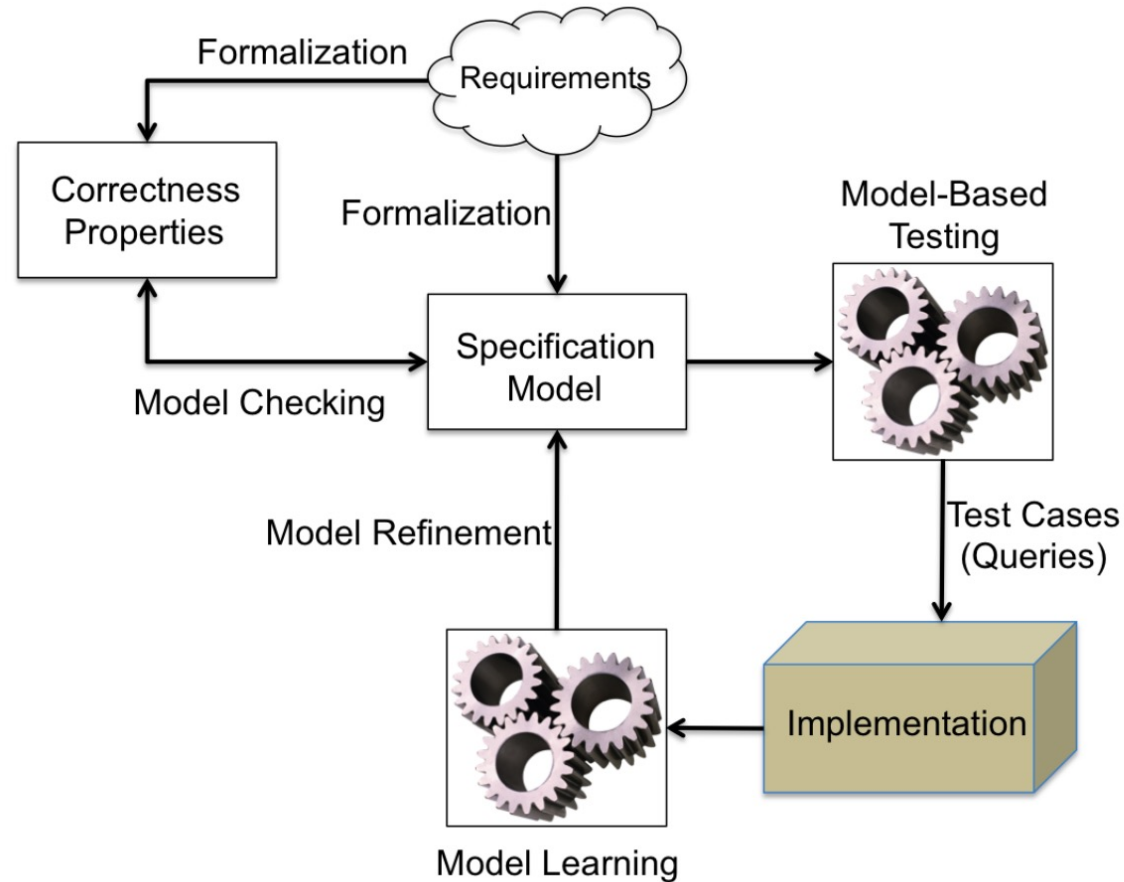


# Active Learning: Why?

Model? What model?

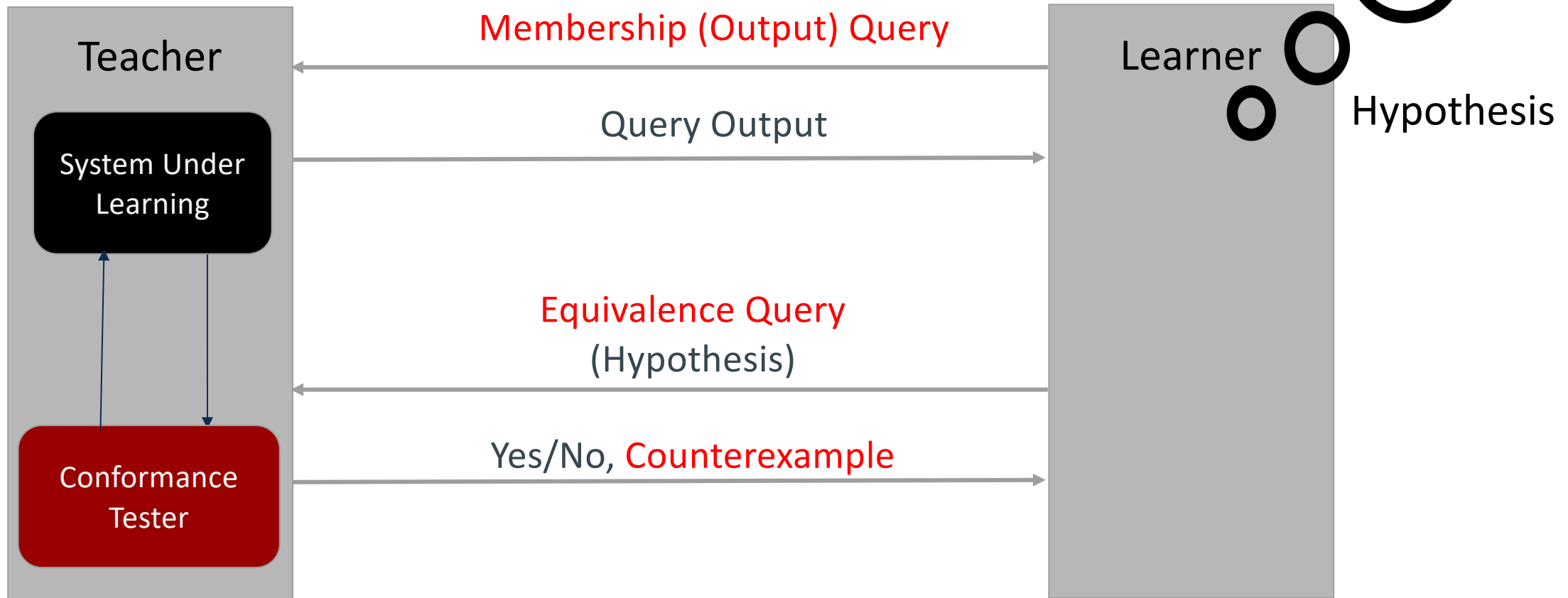


# Active Learning: Why?



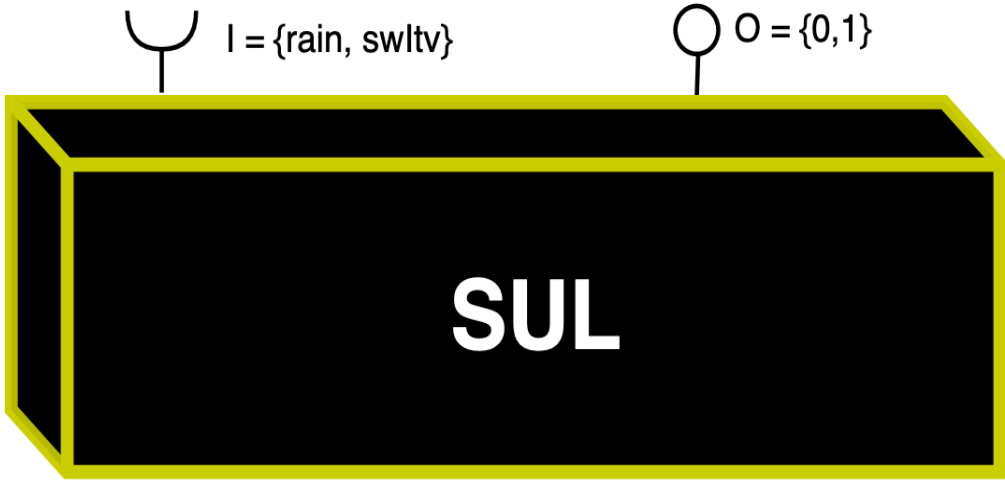
- [Aichernig, et al. Model Learning and Model-Based Testing]
- [Howar and Steffen. Active Automata Learning in Practice]
- [Vaandrager. Model Learning]

# Active Learning: What?



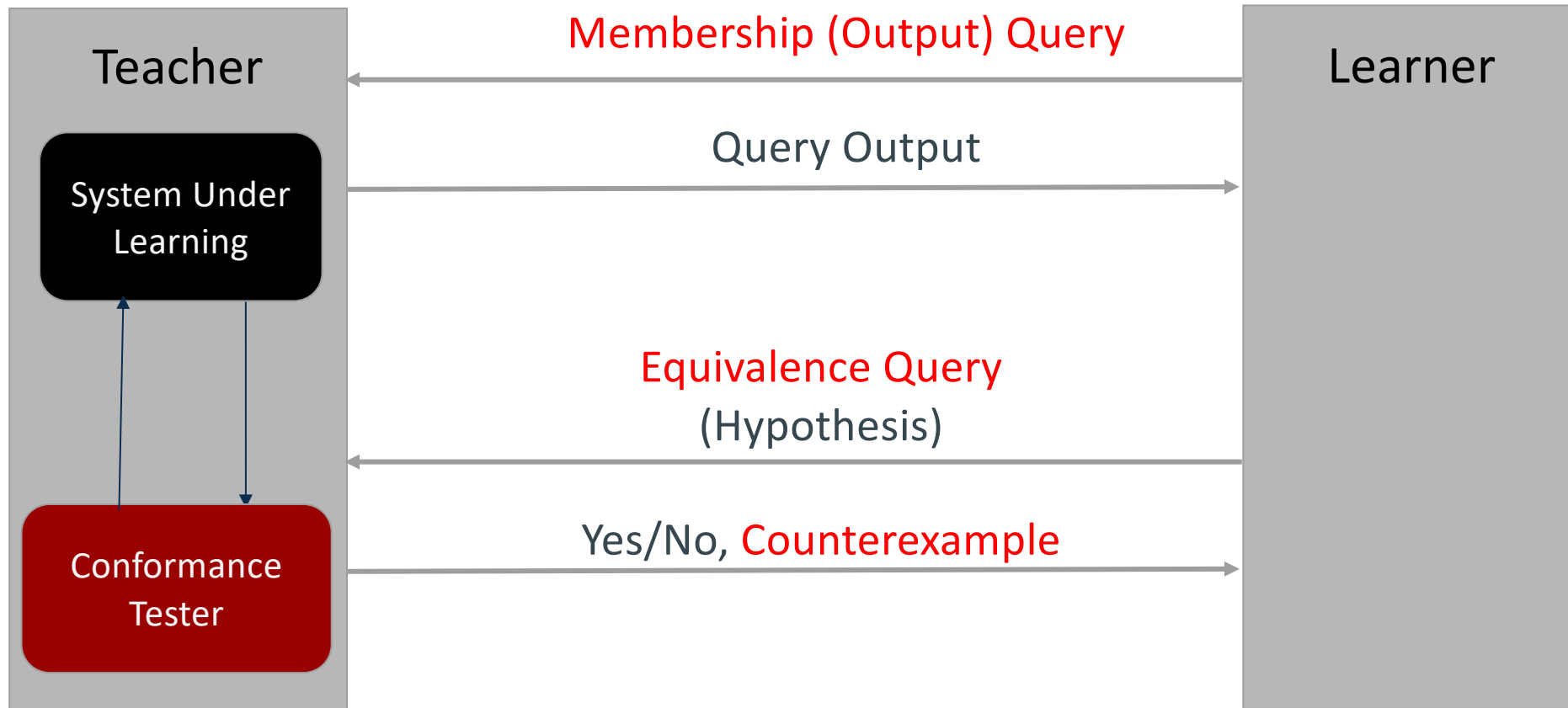
[Dana Angluin. Learning regular sets from queries and counterexamples. I&C. 1987]

# Active Learning: How?

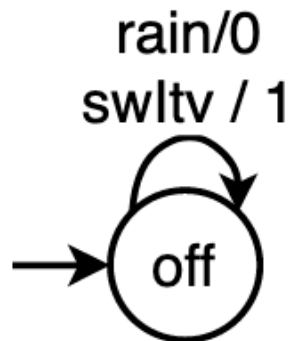
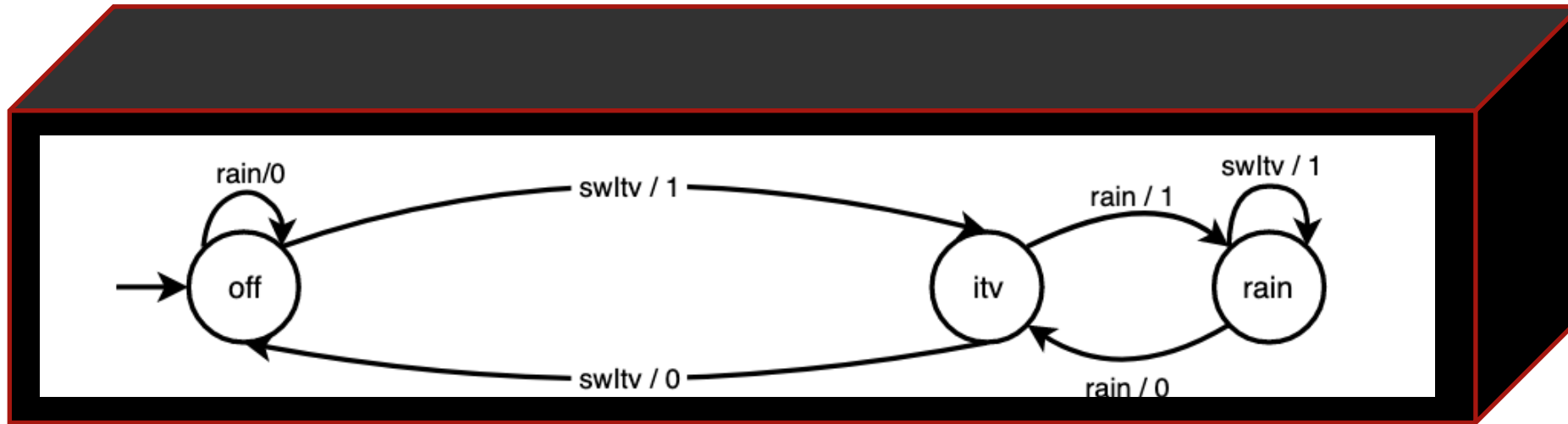




# Active Learning: What?

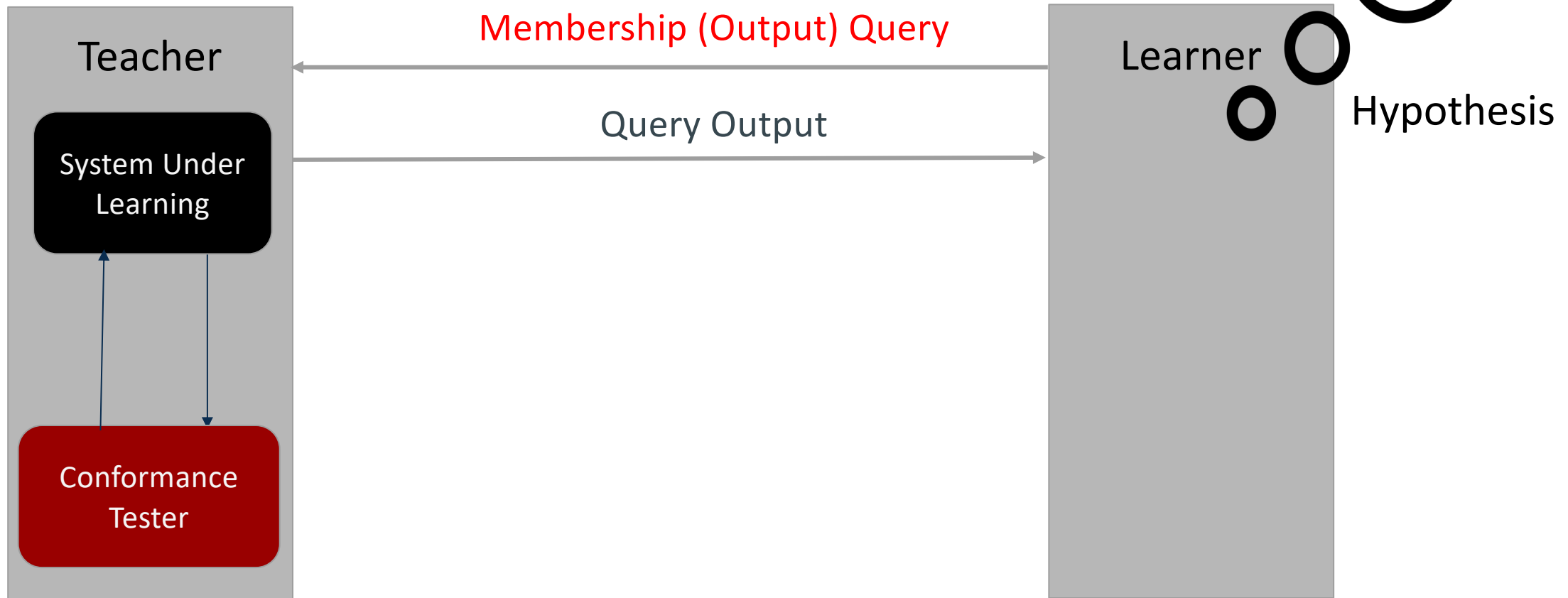


# Active Learning: How?



		rain	swItv
S	€	0	1

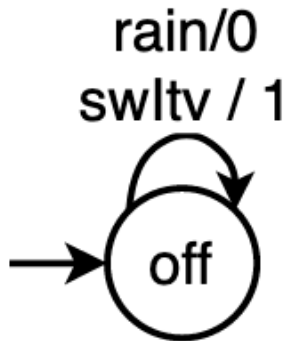
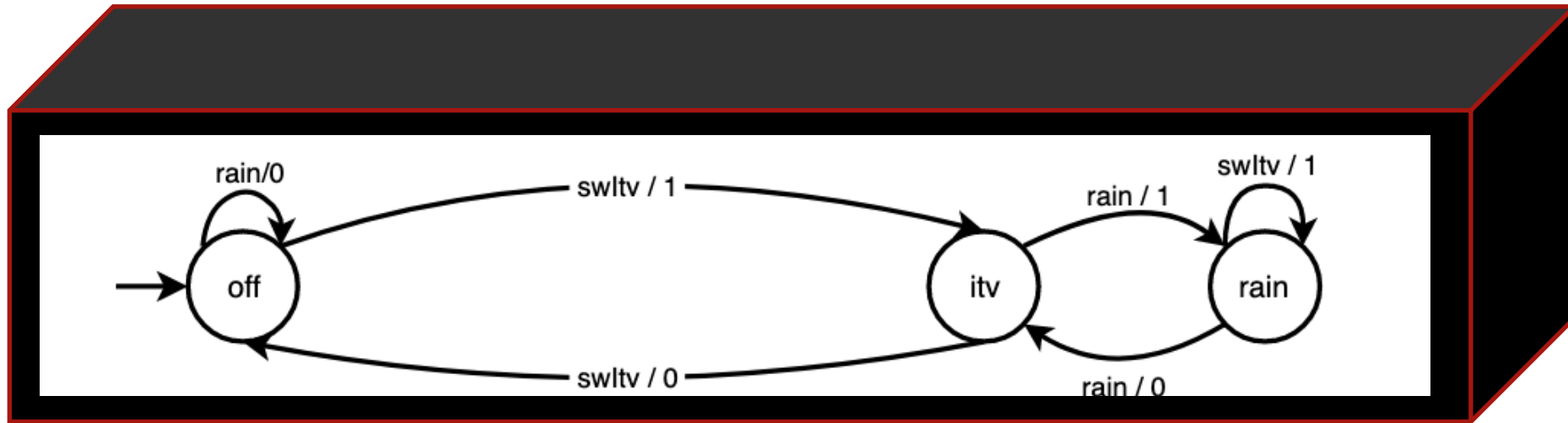
# Active Learning: What?



Good hypothesis?

Can I check that before asking the teacher an equivalence query?

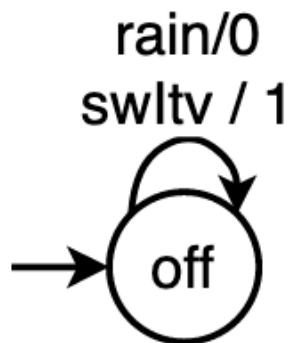
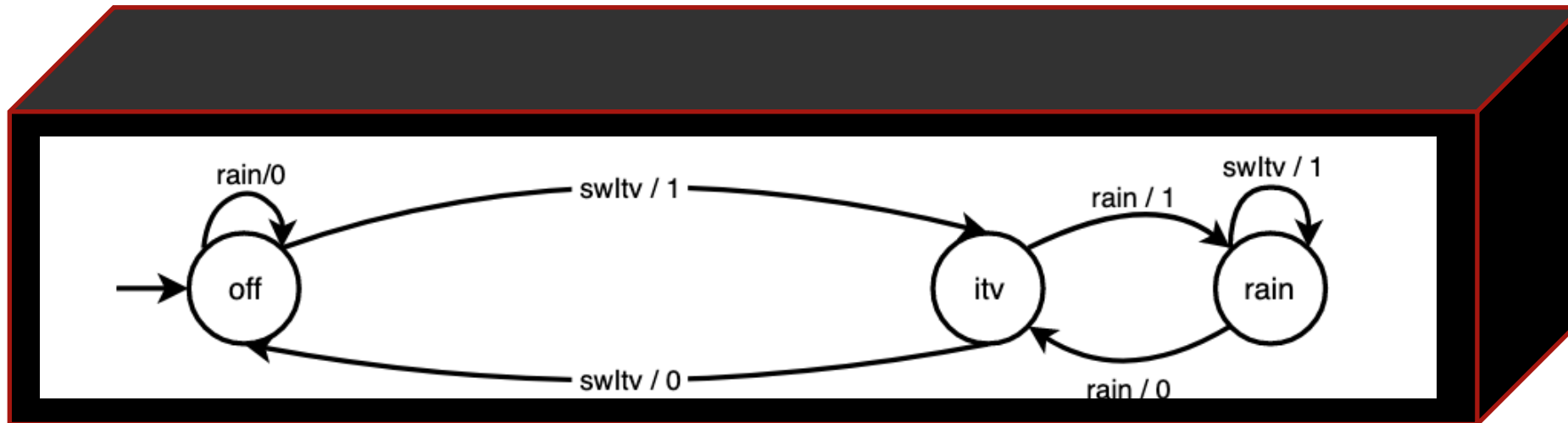
# Active Learning: How?



		rain	swl tv
S	ε	0	1

Consistent:  $\forall p, p' \in S_r \cdot p \cong p' \Rightarrow \forall i \in I \cdot p.i \cong p'.i$

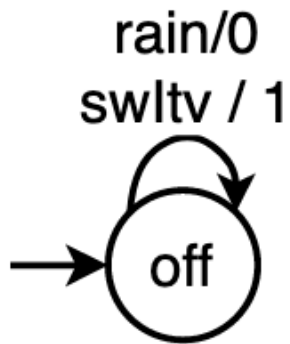
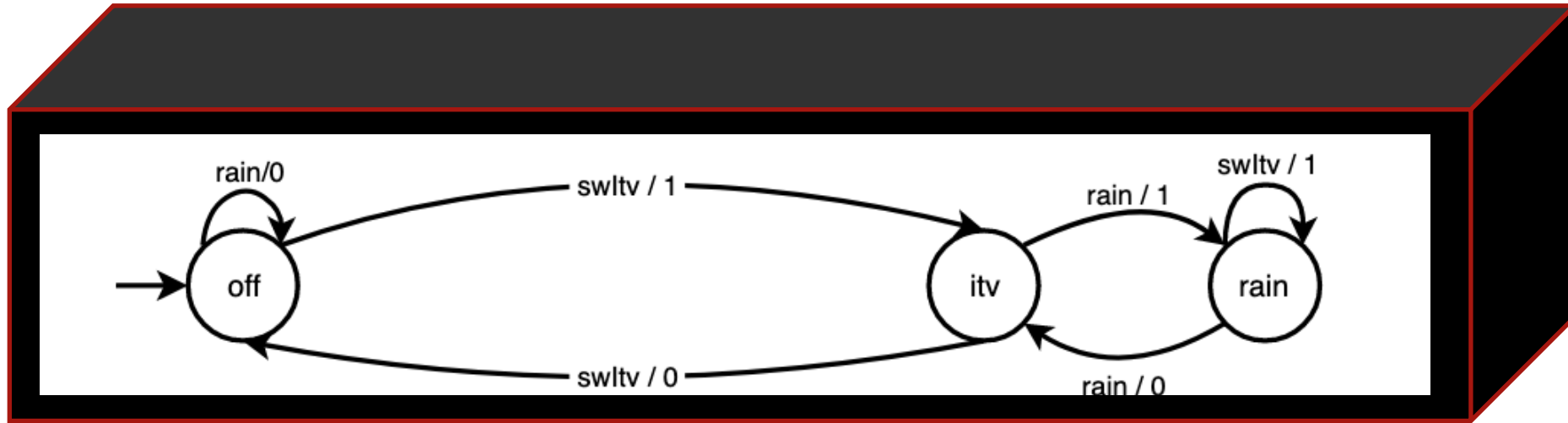
# Active Learning: How?



		rain	swItv
$S$	$\epsilon$	0	1
$S \cdot I$	rain	0	1
	swItv	1	0

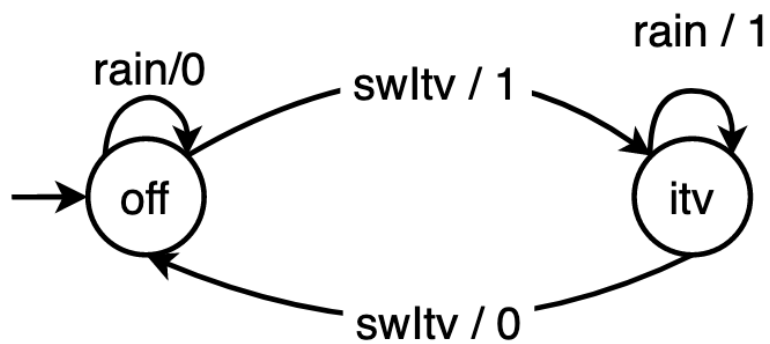
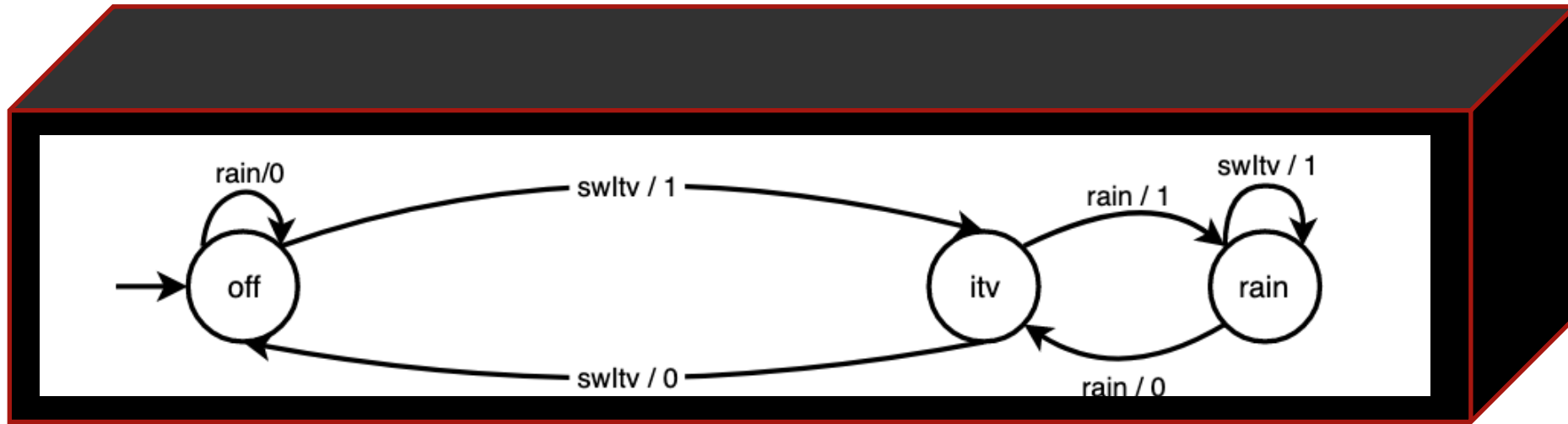
Consistent:  $\forall p, p' \in S_r \cdot p \cong p' \Rightarrow \forall i \in I \ p.i \cong p'.i$

# Active Learning: How?

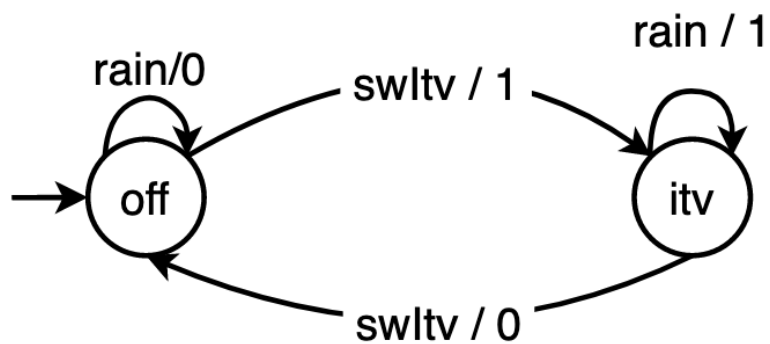
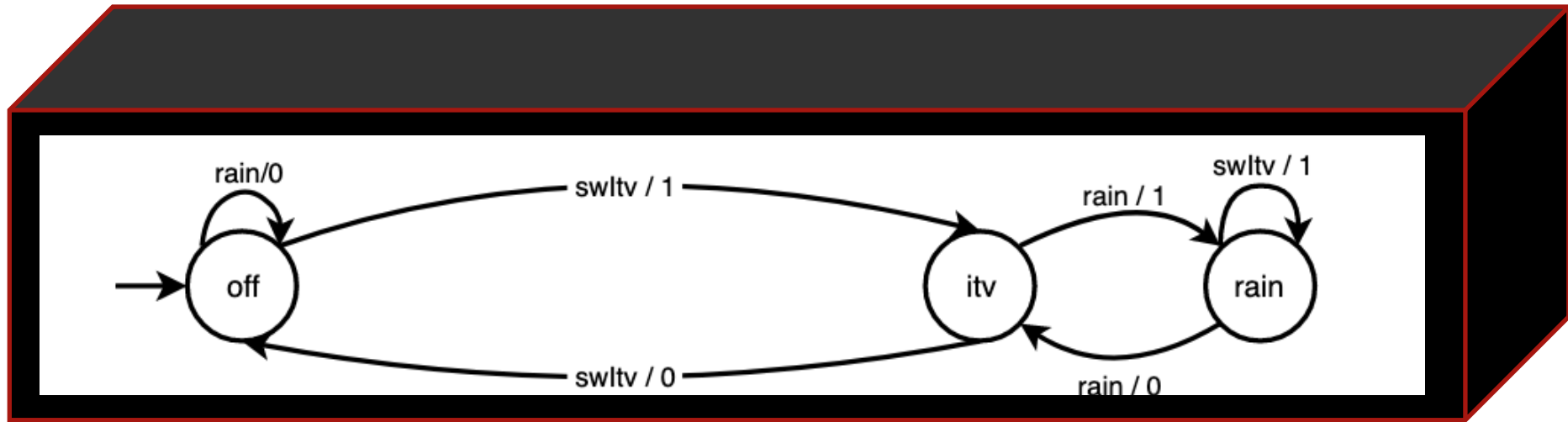


		rain	swItv
$S$	$\epsilon$	0	1
$S \cdot I$	rain	0	1
	swItv	1	0

# Active Learning: How?



		rain	swItv
S	$\epsilon$ ( $\{\epsilon, \text{rain}\}$ )	0	1
	swItv	1	0



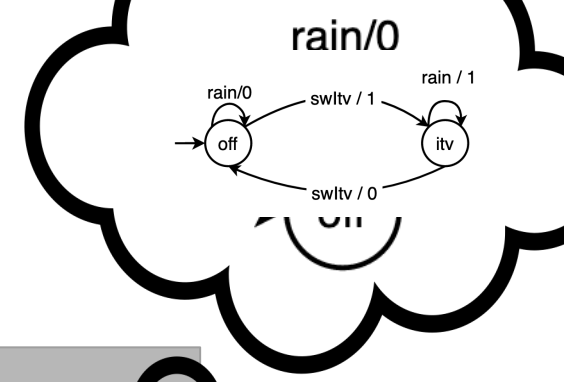
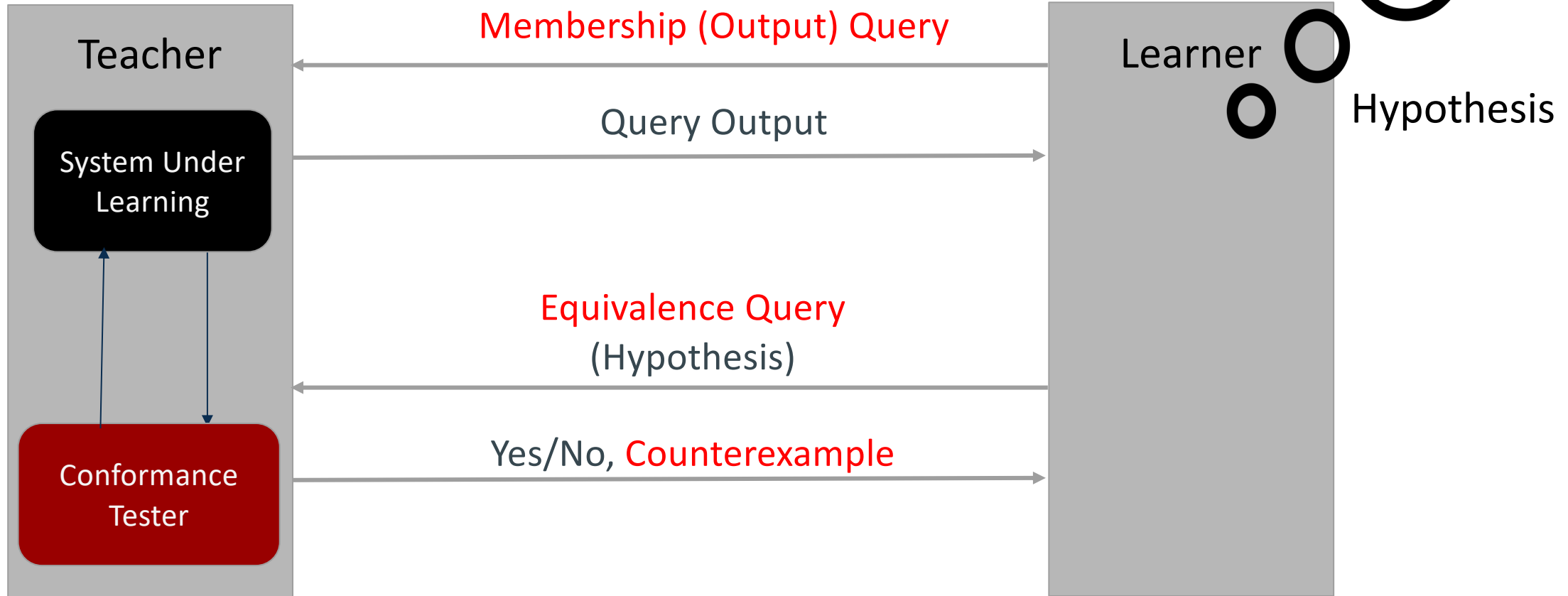
		rain	swl tv
$S$	$\epsilon$ ( $\{\epsilon, \text{rain}\}$ )	0	1
	swl tv	1	0
$S \cdot I$	rain	0	1
	swl tv · rain	0	1
	swl tv · swl tv	0	1

Consistent:  $\forall p, p' \in S_r \cdot p \cong p' \Rightarrow \forall i \in I \ p.i \cong p'.i$

Closed (Complete):  $\forall p \in S_r \cdot I_r \ \exists p' \in S_r \cdot p \cong p'$



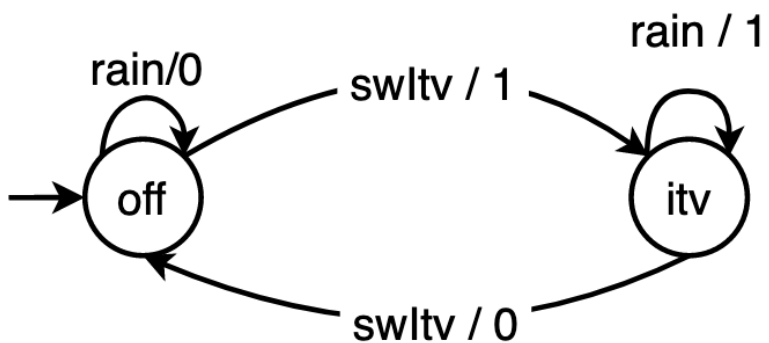
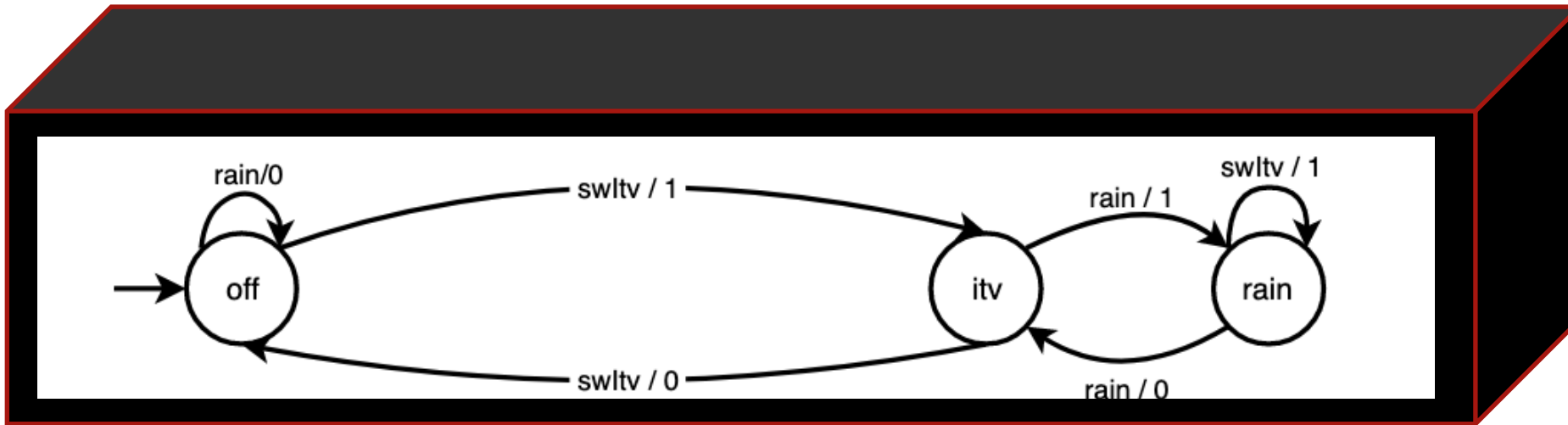
# Active Learning: What?



# Equivalence Queries

- **Random walk**: surprisingly **efficient**, **no guarantees**
- **Complete model-based tests** (W Method, WP Method):
  - Two major phases:
    - establishing a **tour of hypothesis states** in the SUL
    - Testing **all pairs of states and inputs**,  
checking for the correct output and target state
  - Proven **guarantee** of detecting all differences wrt. a given **fault model**

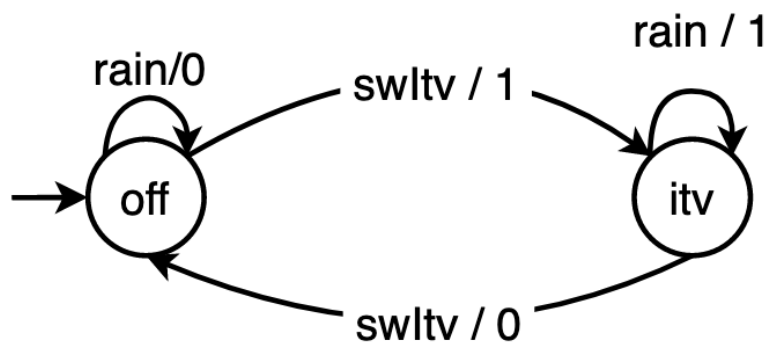
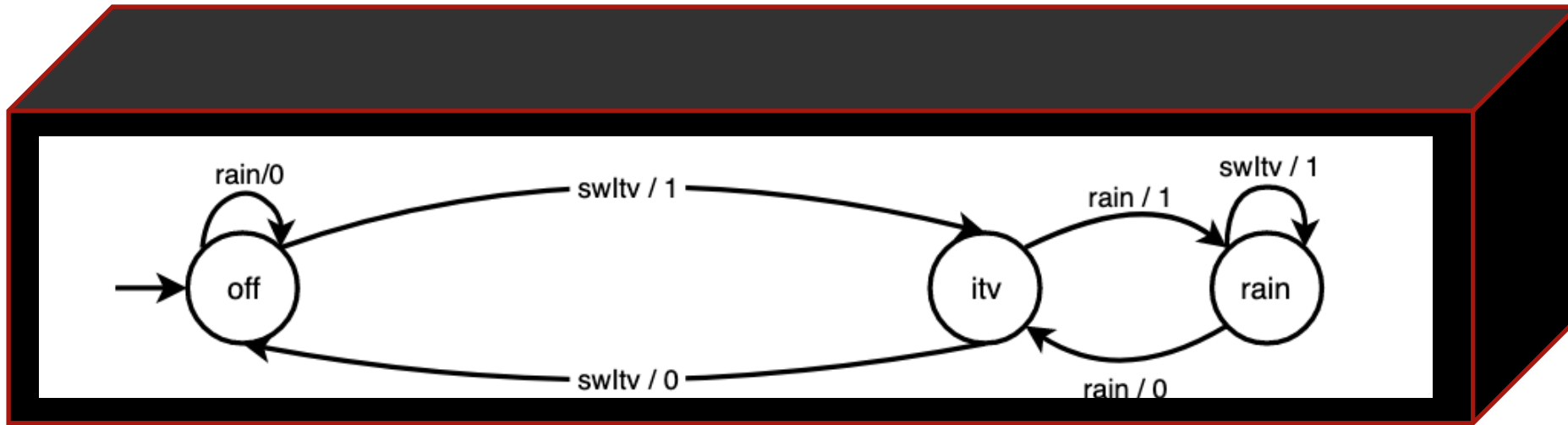
[Broy, Jonsson, Katoen, Leucker, and Pretschner. *Model-Based Testing of Reactive Systems*]



		rain	swItv
$S$	$\epsilon$ ( $\{\epsilon, \text{rain}\}$ )	0	1
	swItv	1	0
$S \cdot I$	rain	0	1
	swItv · rain	0	1
	swItv · swItv	0	1

CE : swItv · rain · rain · rain

How should we process CE?

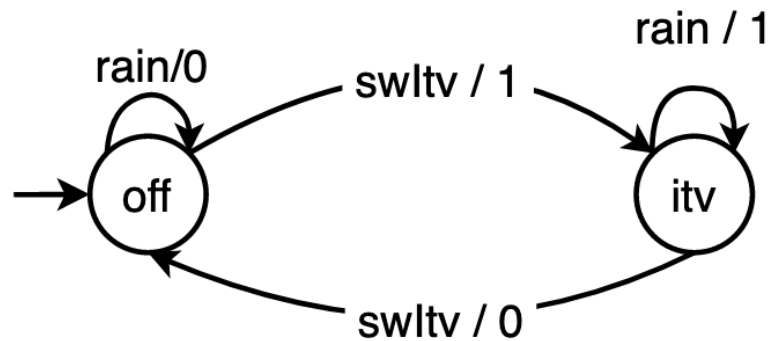
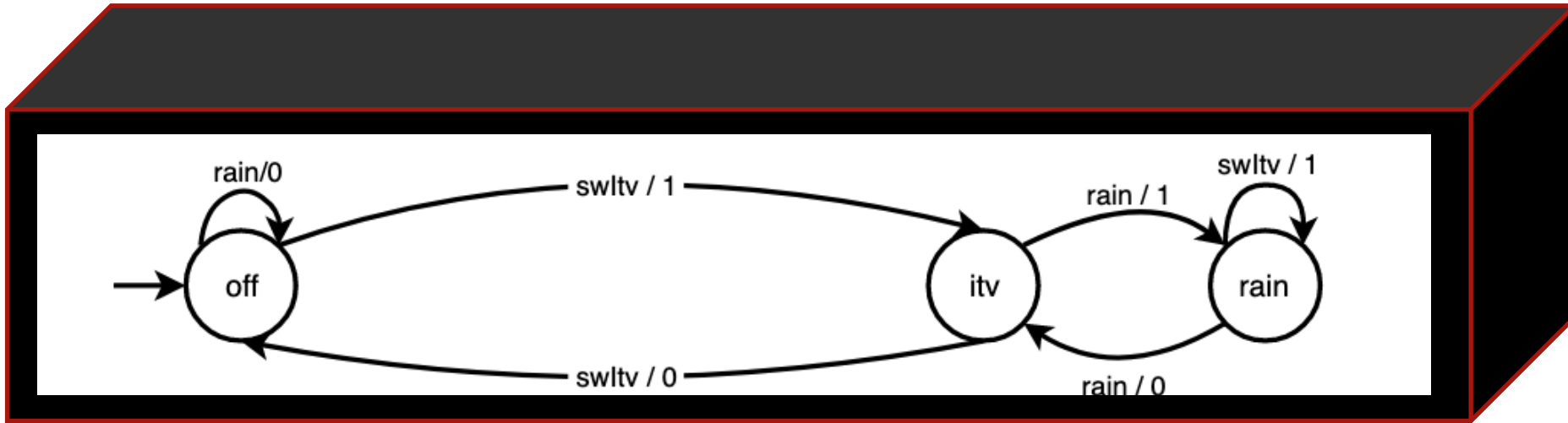


		rain	swItv
$S$	$\epsilon$ ( $\{\epsilon, \text{rain}\}$ )	0	1
	swItv	1	0
$S \cdot I$	rain	0	1
	swItv · rain	0	1
	swItv · swItv	0	1

$$EQ = \text{swItv} \cdot \text{rain} \cdot \text{rain} \cdot \text{rain}$$

$$1 \cdot 1 \cdot 1 \cdot 1 \neq 1 \cdot 1 \cdot 0 \cdot 1$$

# Counter-Example Processing

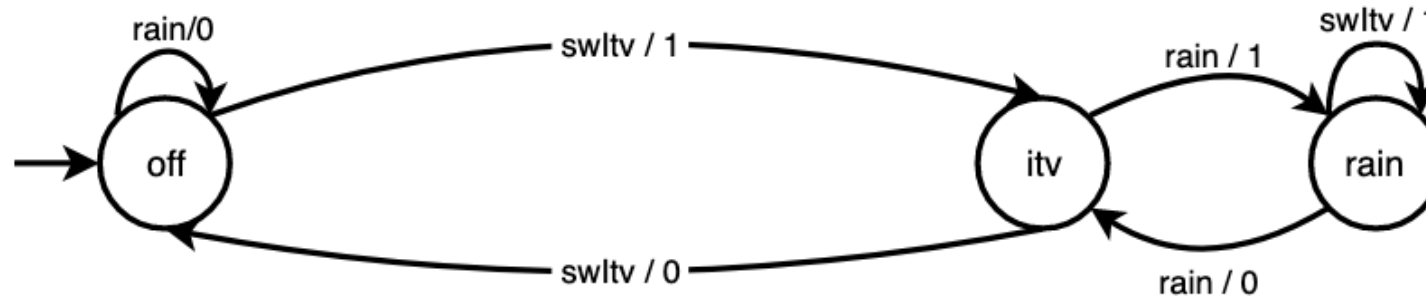


$$\begin{aligned} EQ &= \text{swItv} \cdot \text{rain} \cdot \text{rain} \cdot \text{rain} \\ 1 \cdot 1 \cdot 1 \cdot 1 &\neq 1 \cdot 1 \cdot 0 \cdot 1 \end{aligned}$$

[Rivest and Schapire. Inference of finite automata using homing sequence. I&C. 1993]

[Irfan, Oriat, Groz. Model Inference and Testing. Adv. Comp. 2013 ]

# Counter-Example Processing

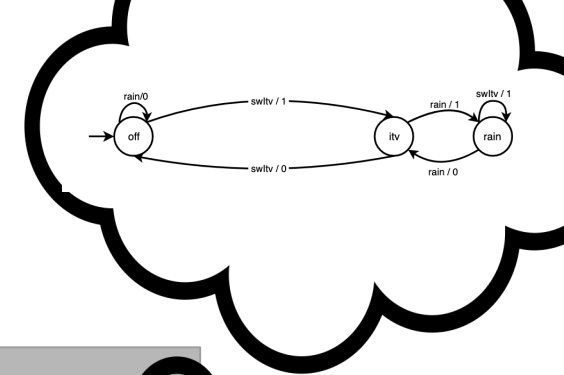
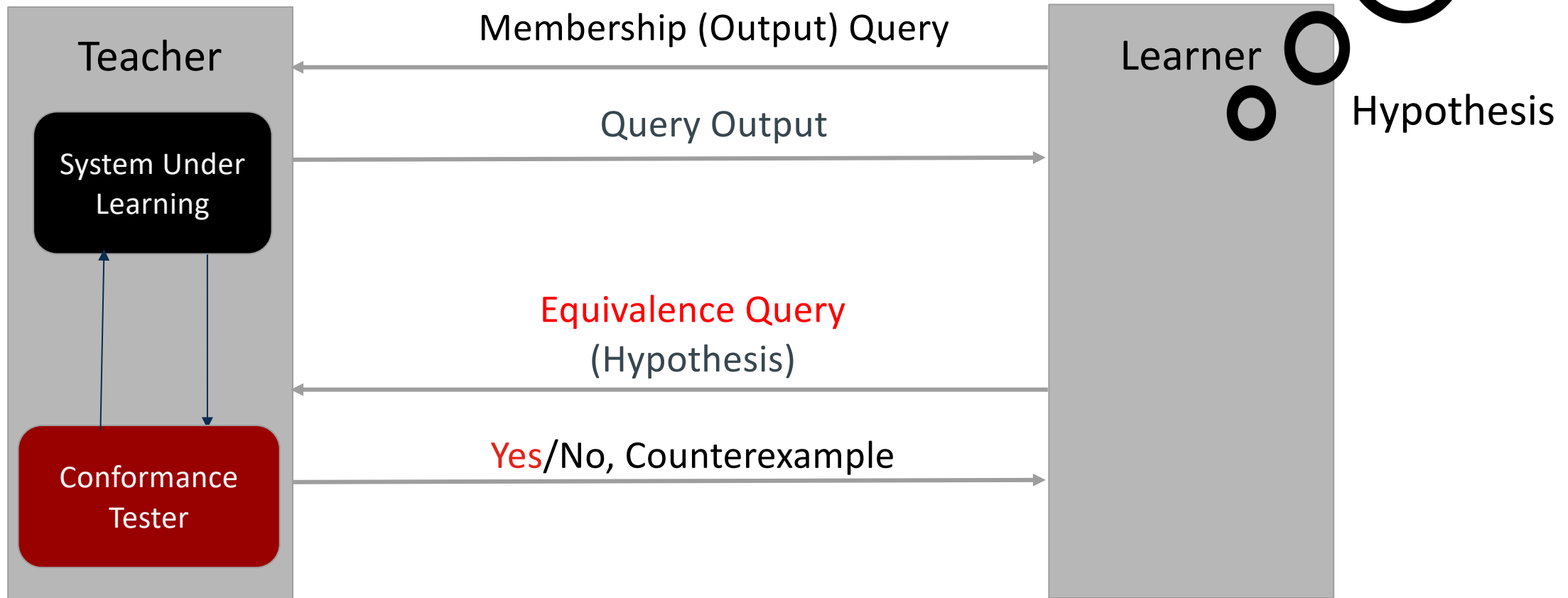


		<i>rain</i>	<i>swltv</i>	<i>rain · rain</i>
$S_r$	$\epsilon$	0	1	0 · 0
	<i>swltv</i>	1	0	1 · 0
	<i>swltv · rain</i>	0	1	0 · 1
$S_r \cdot I_r$	<i>rain</i>	0	1	0 · 0
	<i>swltv · swltv</i>	0	1	0 · 0
	<i>swltv · rain · rain</i>	1	0	1 · 0
	<i>swltv · rain · swltv</i>	0	1	0 · 1

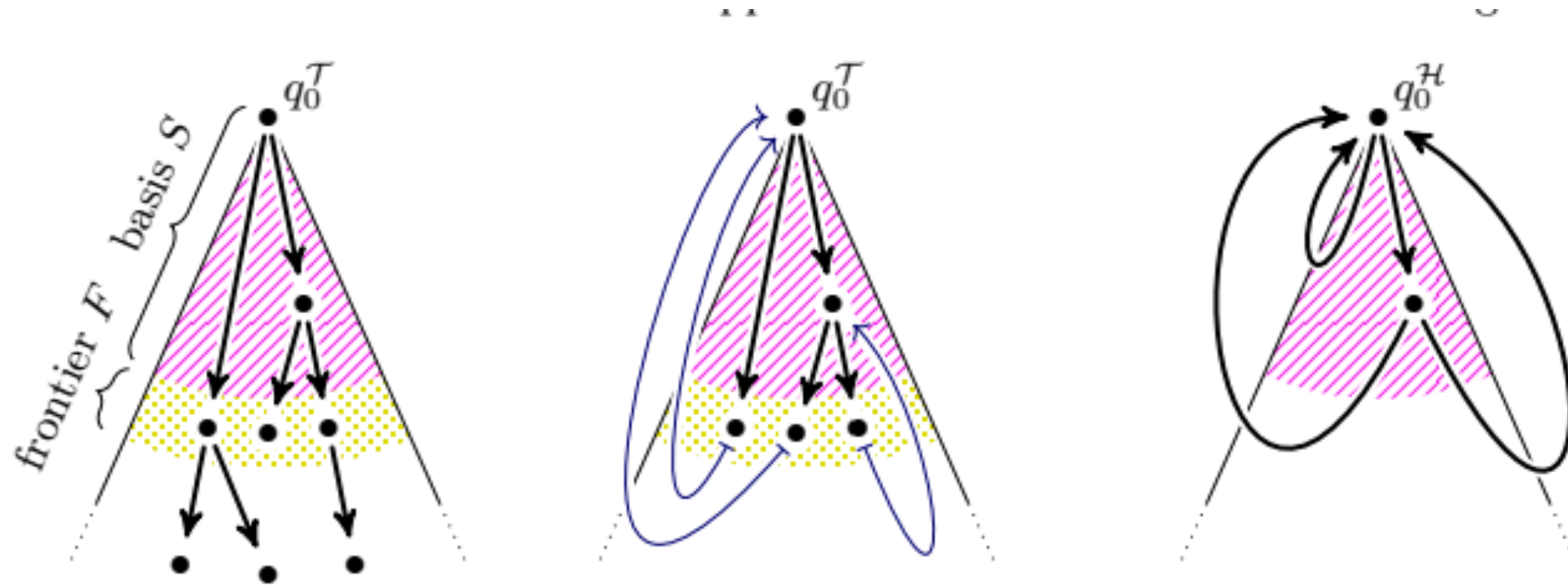
[Rivest and Schapire. Inference of finite automata using homing sequence. I&C. 1993]

[Irfan Oriat, Groz. Angluin-style finite-state machine inference with non-optimal counter-examples.]

# Active Learning: What?



# Beyond $L^*$

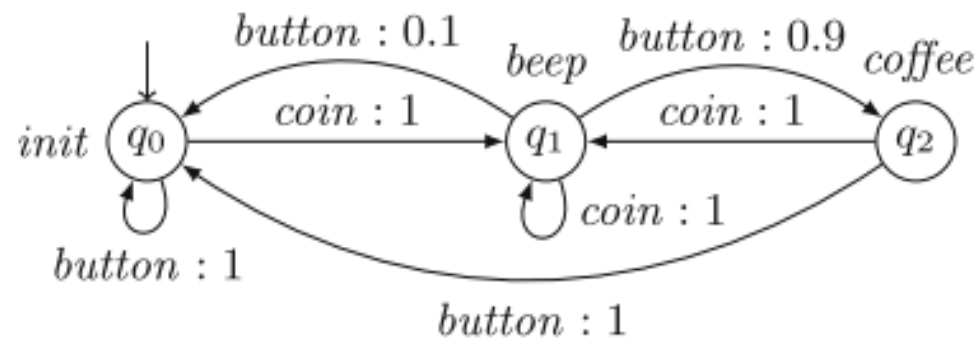


[M. Isberner. Foundations of Active Automata Learning An Algorithmic Perspective. Ph.D. Thesis. 2015]

[Vaandrager et al. A New Approach for Active Automata Learning Based on Apartness.]



# Beyond Finite Automata



		<i>button</i>	<i>coin</i>
<i>S</i>	$\epsilon$	{ <i>init</i> : 247}	{ <i>beep</i> : 414}
	<i>coin</i> · <i>beep</i>	{ <i>coffee</i> : 147, <i>init</i> : 16}	{ <i>beep</i> : 134}
<i>Lt(S)</i>	<i>button</i> · <i>init</i>	{ <i>init</i> : 69}	{ <i>beep</i> : 82}
	<i>coin</i> · <i>beep</i> · <i>button</i> · <i>coffee</i>	{ <i>init</i> : 64}	{ <i>beep</i> : 53}
	<i>coin</i> · <i>beep</i> · <i>button</i> · <i>init</i>	{ <i>init</i> : 9}	{ <i>beep</i> : 6}
	<i>coin</i> · <i>beep</i> · <i>coin</i> · <i>beep</i>	{ <i>coffee</i> : 65, <i>init</i> : 7}	{ <i>beep</i> : 61}

[Tappler, Muškardin, Aichernig, Pill. Active Model Learning for Stochastic Automata.]

[Bacci, Ingolfsdottir, Larsen, Reynouard. Active Learning of Markov Decision Processes using Baum Welch Algorithm.]



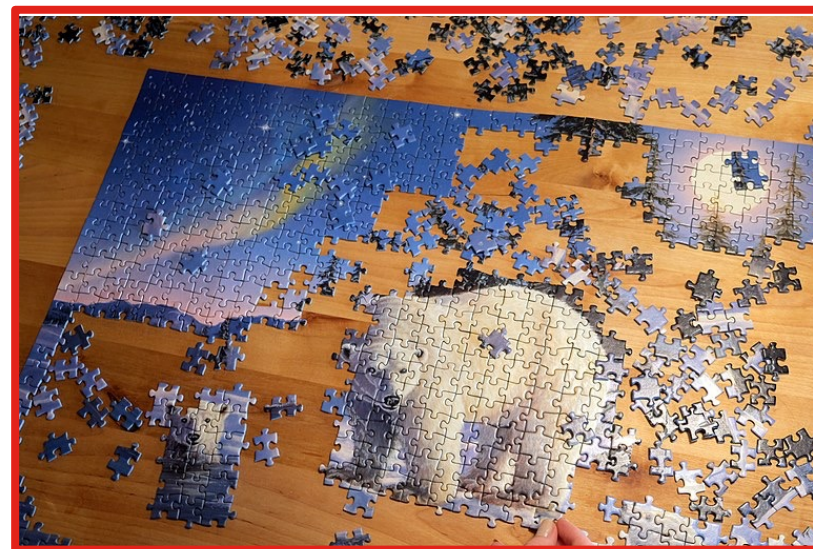
**Active Automata Learning**



**Adaptive Learning**



**Learning Evolution in Space**

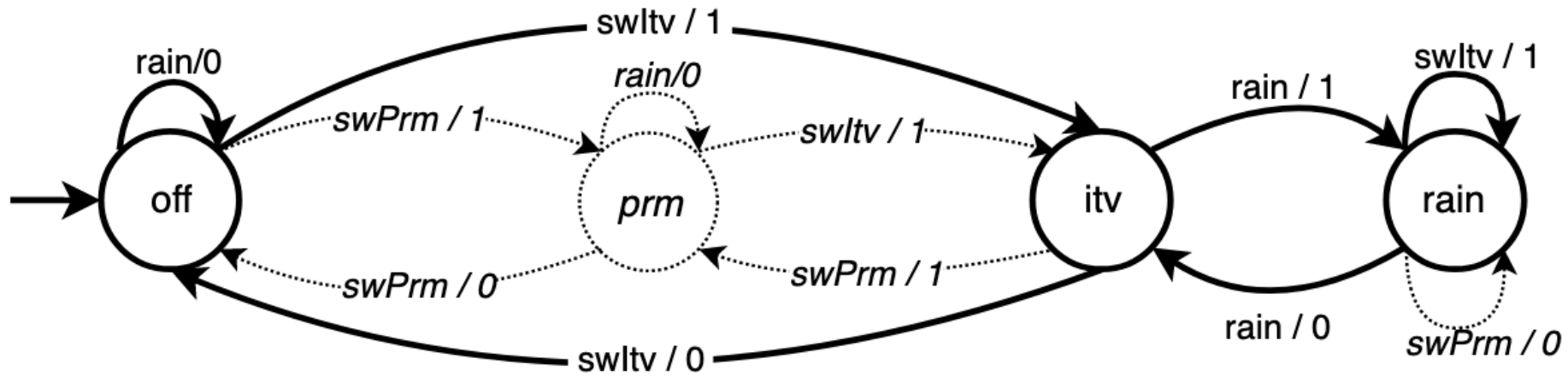
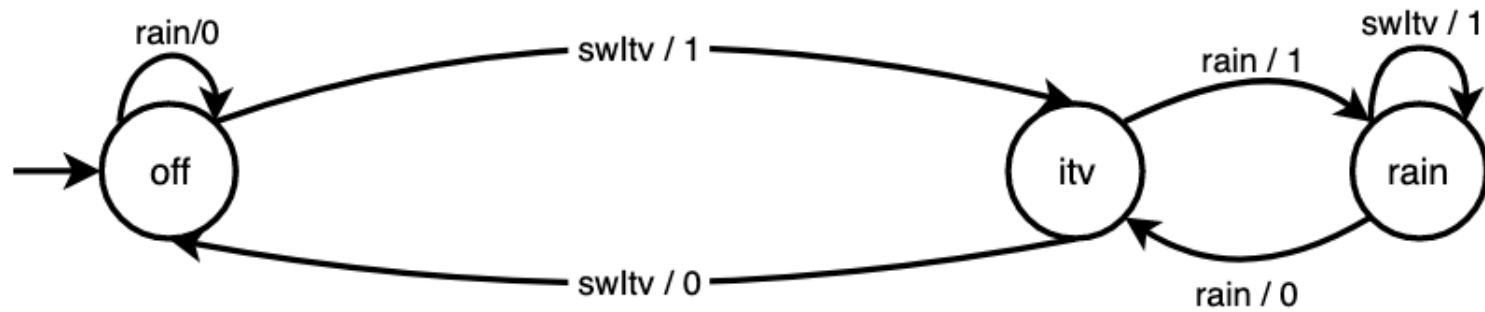


**Compositional Learning**

# Adaptive Learning



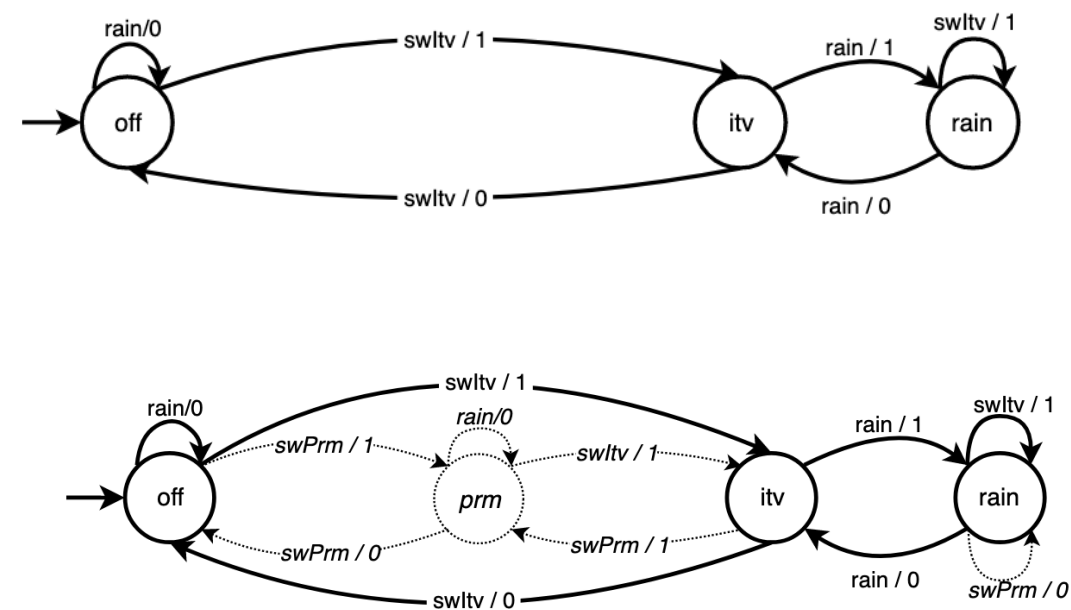
# Why?



# What?

Given an **evolving system** that changed over time  
how can we **efficiently**  
learn its **evolved behavior**?

How **sensitive** is it to  
the amount of **evolution**?

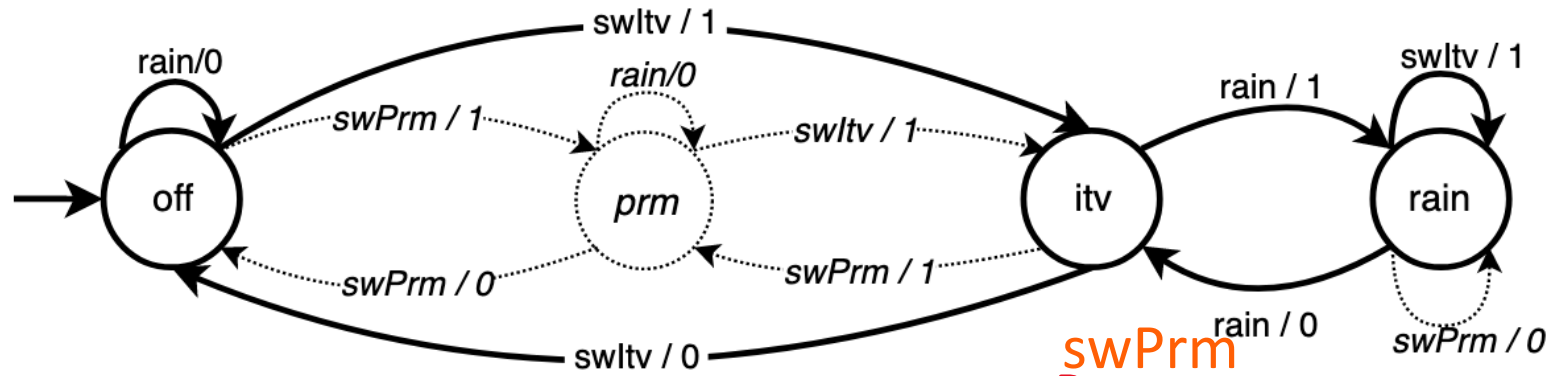


[Groce, Peled, and Yannakakis. Adaptive model checking. 2002]

[Chaki, Clarke, Sharygina, Sinha.

Verification of evolving software via component substitutability analysis. 2008]

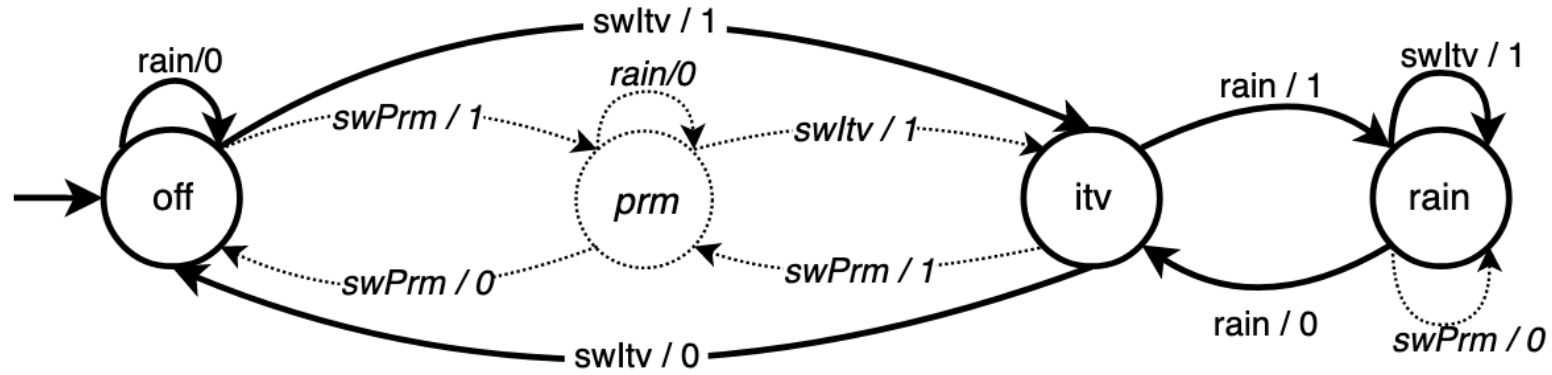
# How?



Anything redundant?

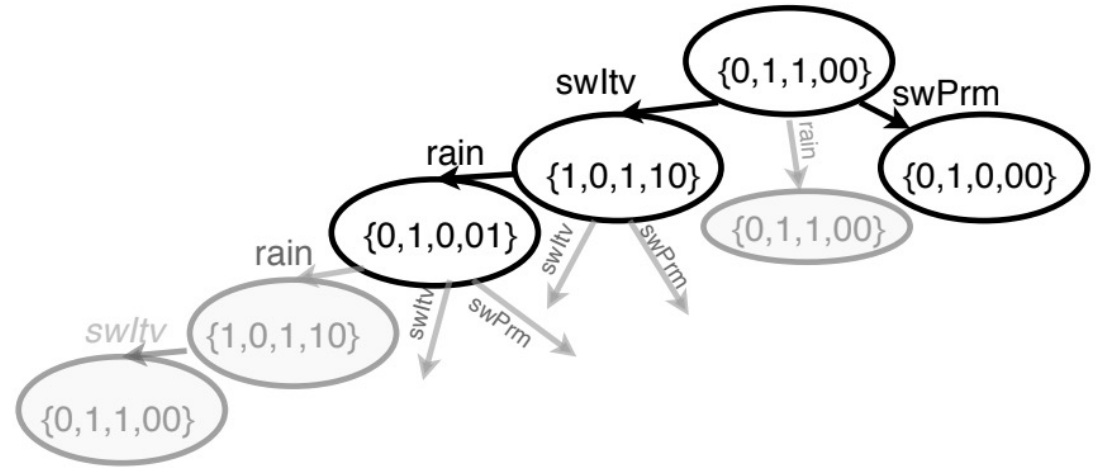
		<i>rain</i>	<i>swItv</i>	<i>rain · rain</i>
$S_r$	$\epsilon$	0	1	0 · 0
	<i>swItv</i>	1	0	1 · 0
	<i>swItv · rain</i>	0	1	0 · 1
$S_r \cdot I_r$	<i>rain</i>	0	1	0 · 0
	<i>swItv · swItv</i>	0	1	0 · 0
	<i>swItv · rain · rain</i>	1	0	1 · 0
	<i>swItv · rain · swItv</i>	0	1	0 · 1

# How?

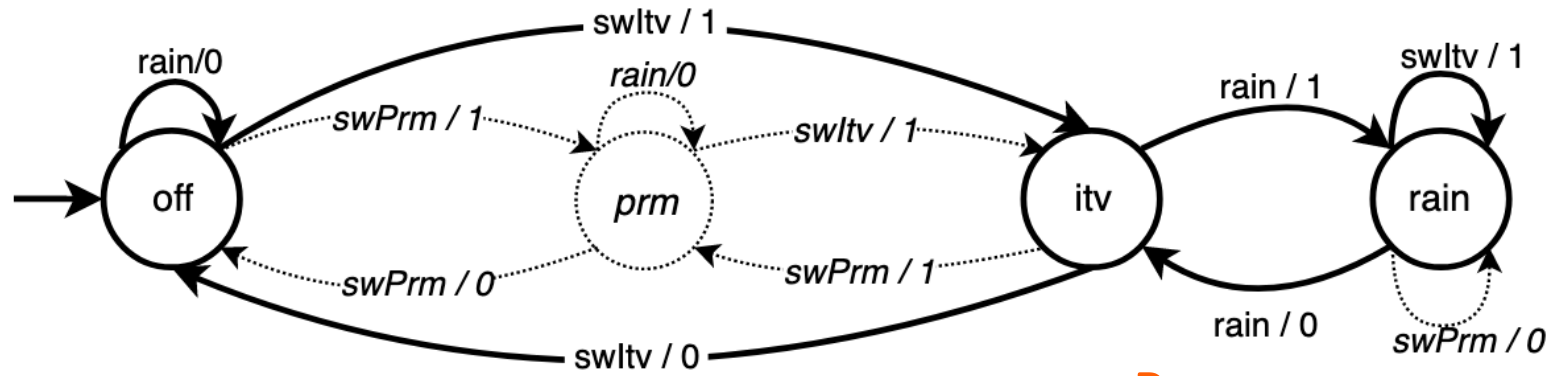


Anything redundant?

		<i>rain</i>	<i>swltv</i>	<i>rain · rain</i>
$S_r$	$\epsilon$	0	1	0 · 0
	<i>swltv</i>	1	0	1 · 0
	<i>swltv · rain</i>	0	1	0 · 1
$S_r \cdot I_r$	<i>rain</i>	0	1	0 · 0
	<i>swltv · swltv</i>	0	1	0 · 0
	<i>swltv · rain · rain</i>	1	0	1 · 0
	<i>swltv · rain · swltv</i>	0	1	0 · 1



# How?



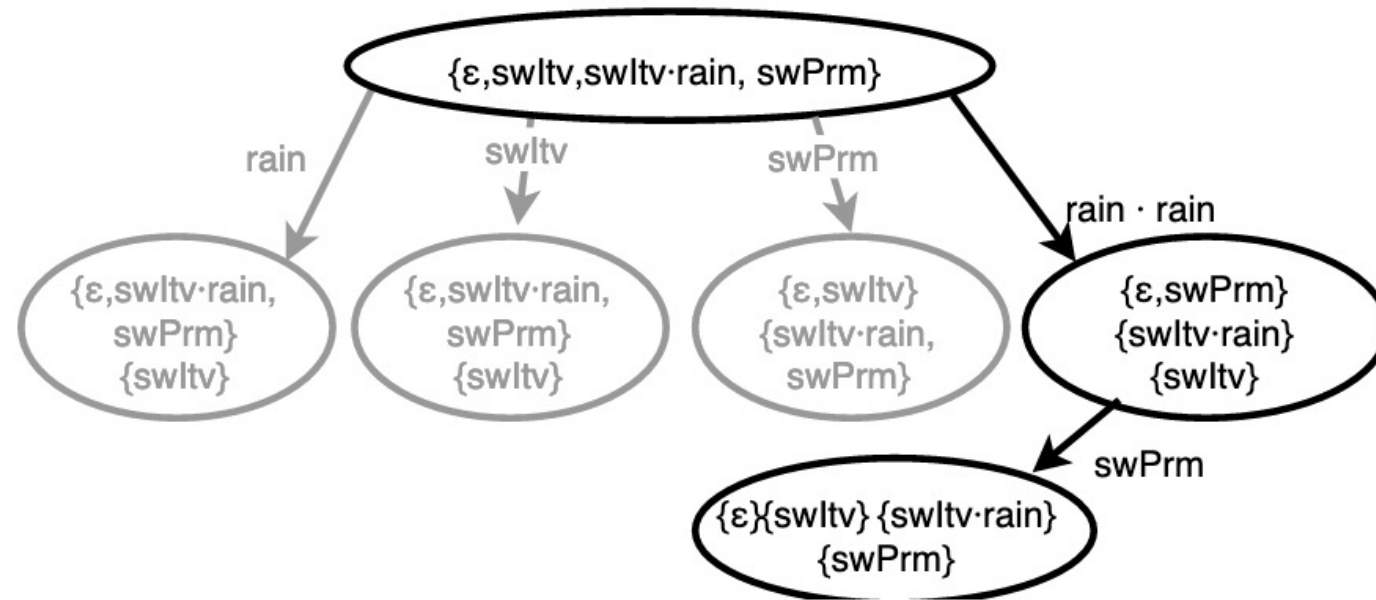
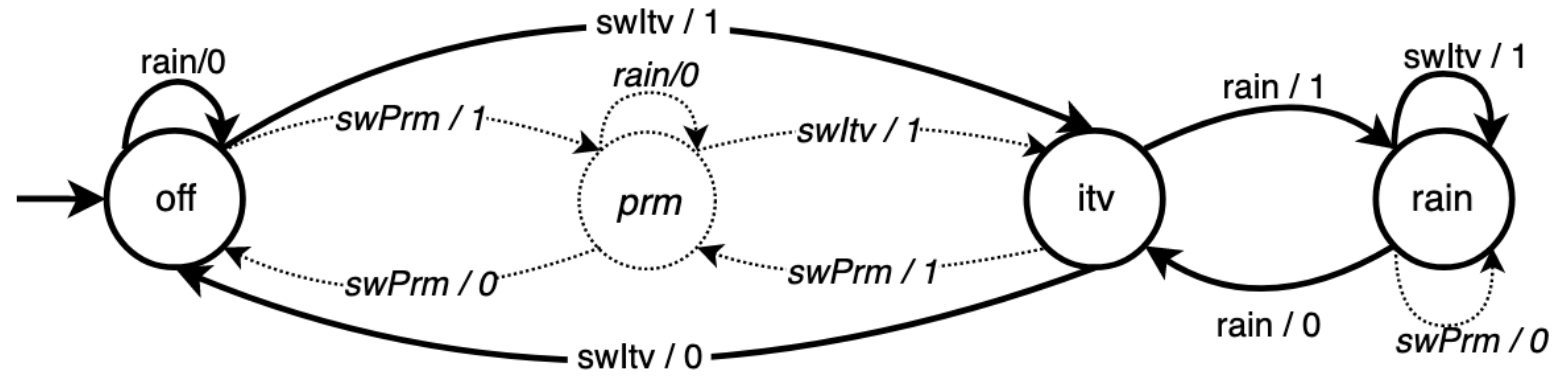
New experiments?

swPrm

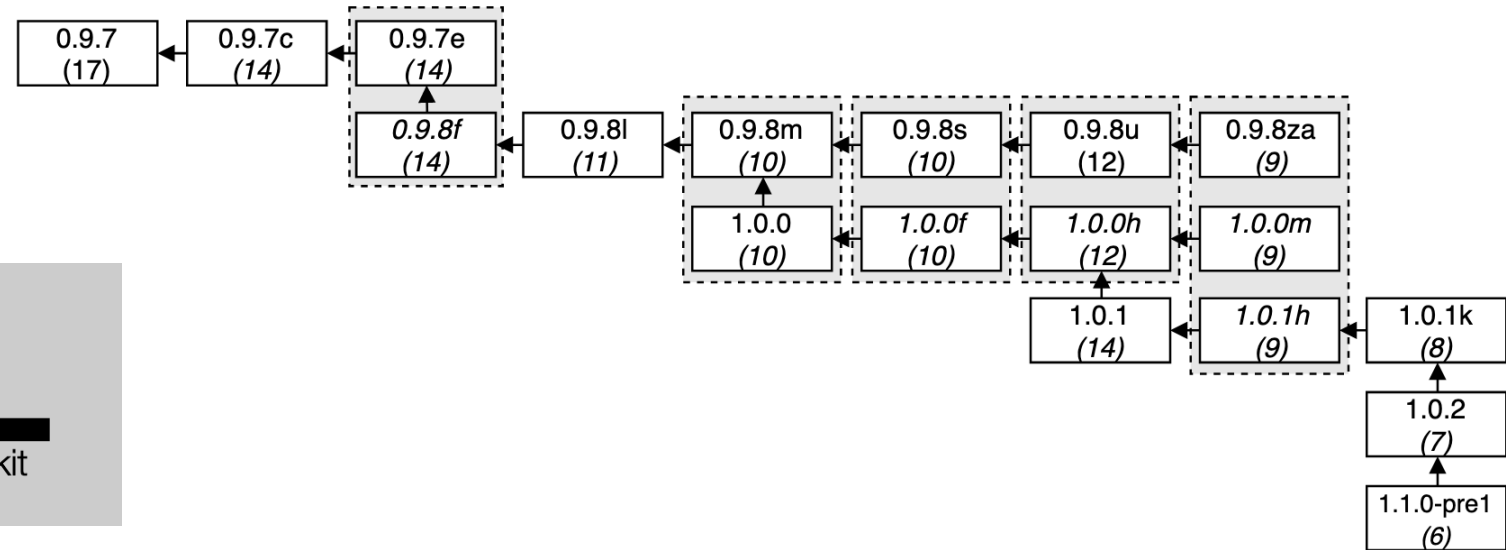
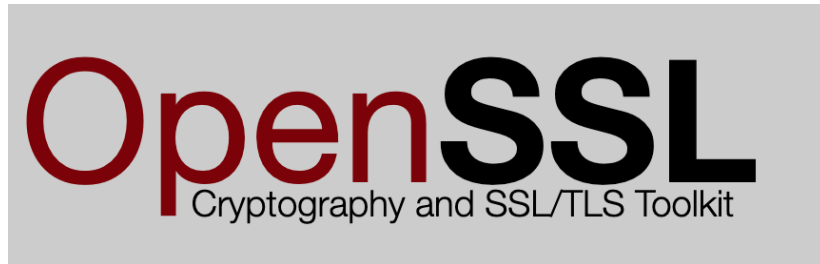
		<i>rain</i>	<i>swItv</i>	<i>rain · rain</i>
$S_r$	$\epsilon$	0	1	0 · 0
	<i>swItv</i>	1	0	1 · 0
	<i>swItv · rain</i>	0	1	0 · 1
$S_r \cdot I_r$	<i>rain</i>	0	1	0 · 0
	<i>swItv · swItv</i>	0	1	0 · 0
	<i>swItv · rain · rain</i>	1	0	1 · 0
	<i>swItv · rain · swItv</i>	0	1	0 · 1



# How?



# Does it Really work?



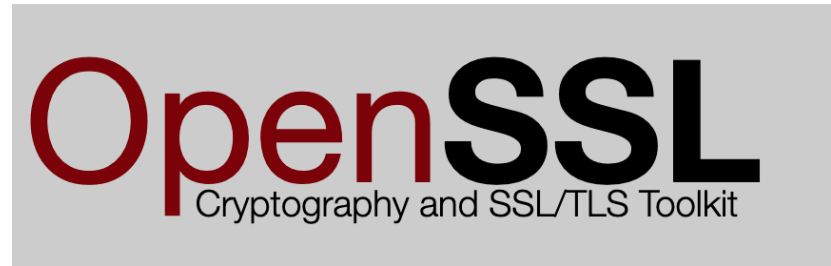
[<https://www.openssl.org/>]

[De Ruiter. A tale of the openssl state machine. 2016 ]

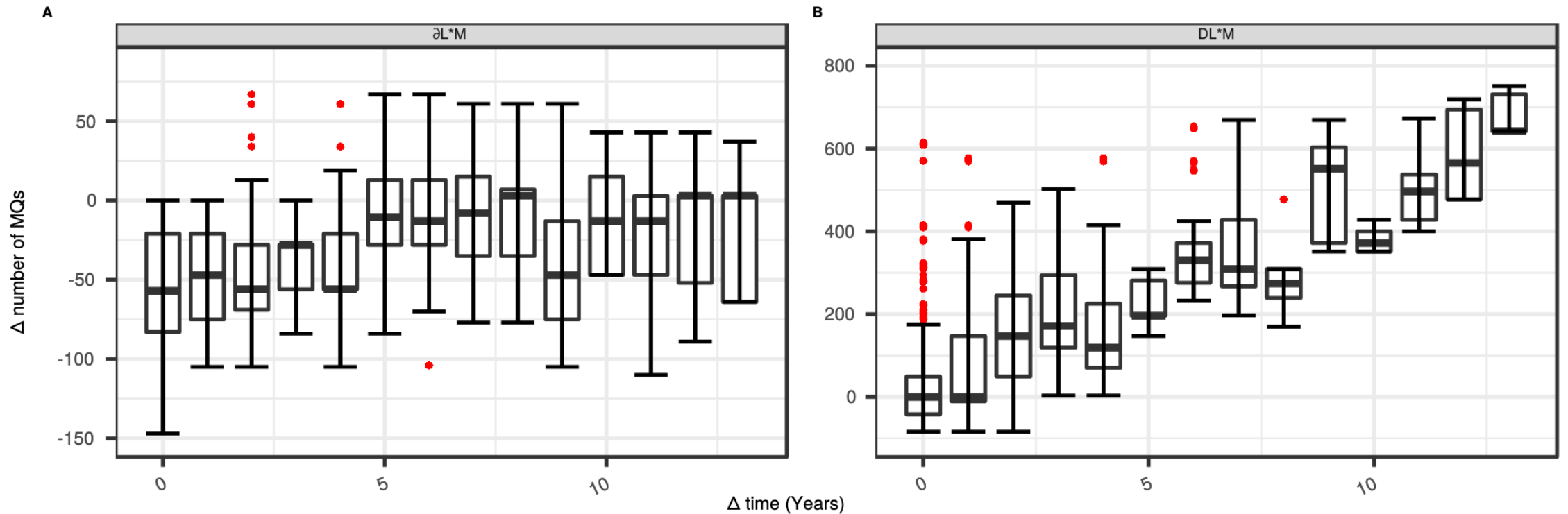
# DOES IT REALLY WORK?

Given an **evolving system** that  
changed over time  
how can we **efficiently**  
learn its **evolved behavior**?

How **sensitive** is it to  
the amount of **evolution**?



# Does it Really work?



[Damasceno, M.R. Mousavi and A. Simao.

[Learning to Reuse: Adaptive Model Learning for Evolving Systems. iFM'19](#) ]



**Active Automata Learning**



**Adaptive Learning**



**Product-Line Learning**

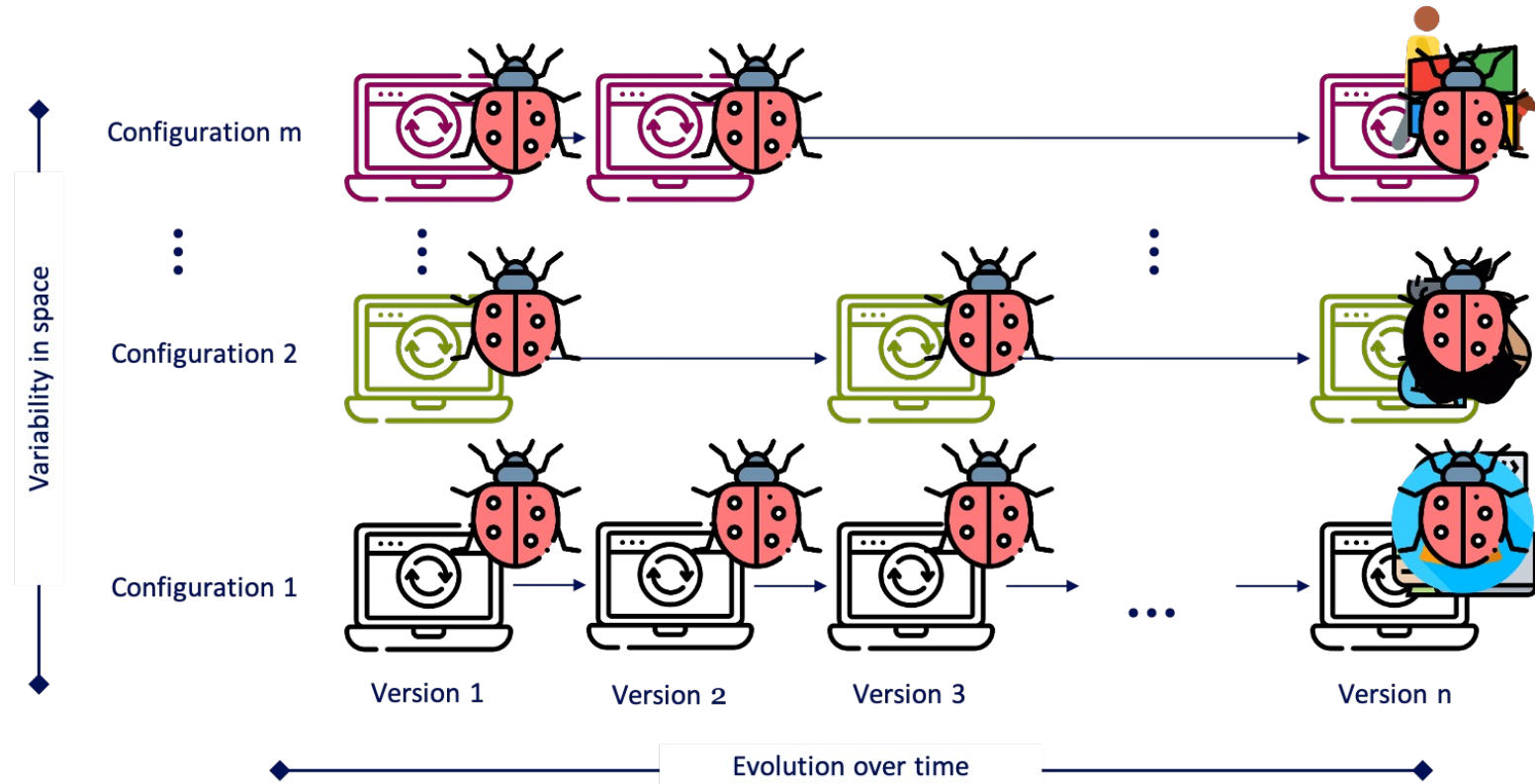


**Compositional Learning**

# Product-Line Learning



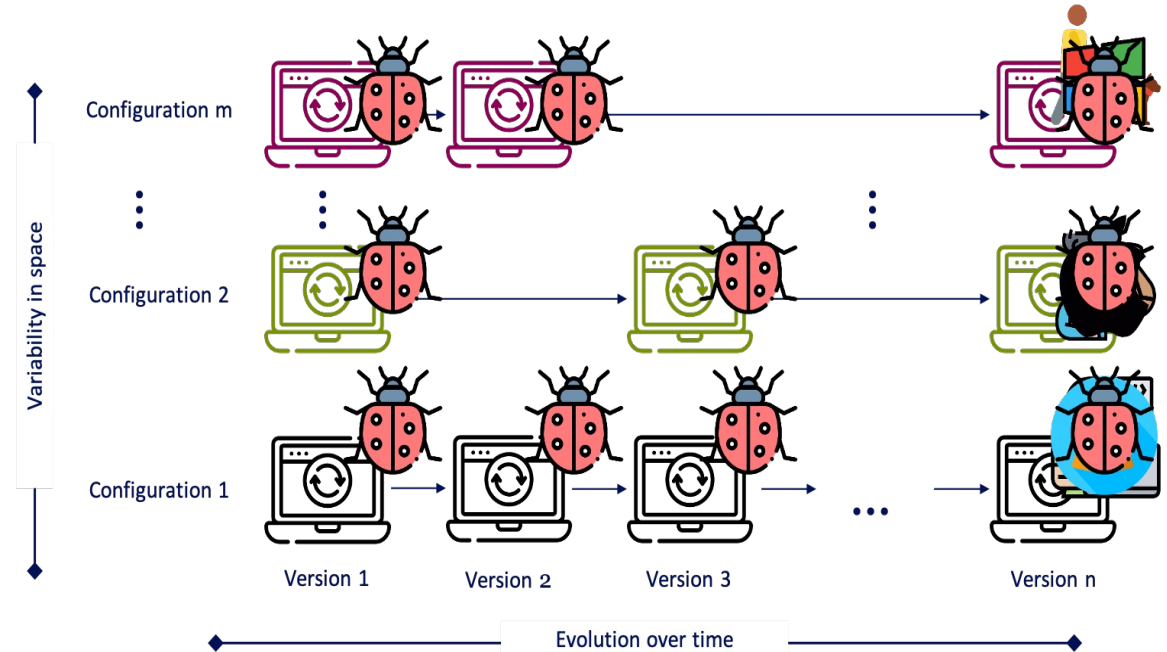
# Why?



# Why?

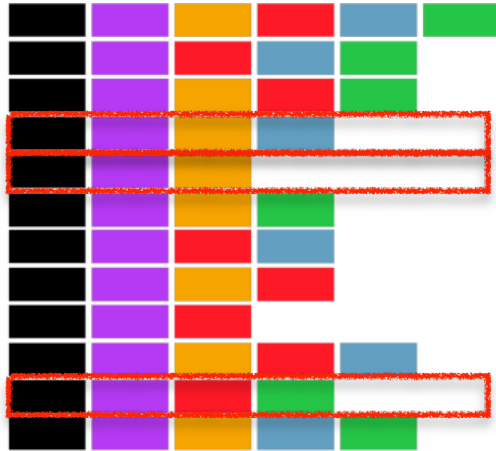
Given an **evolving system** that changed in **space** how can we **succintly** summarise the **variability**?

How **sensitive** is it to the number of configuration **samples**?

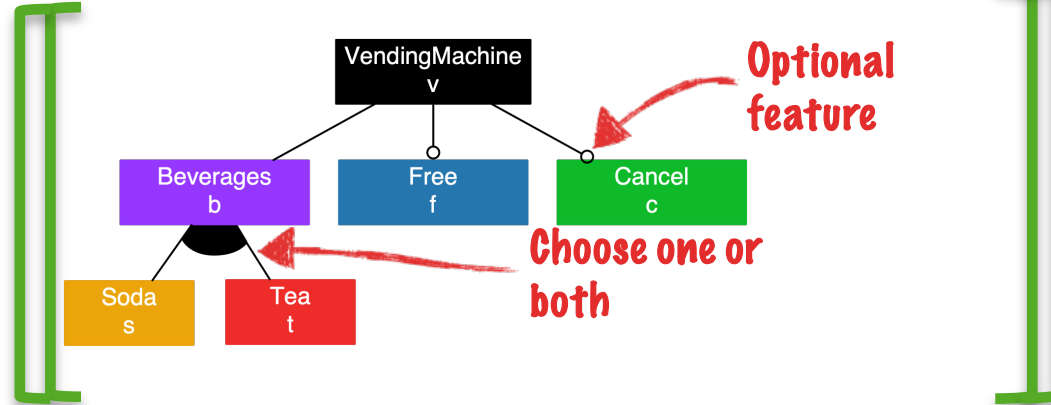




# What?

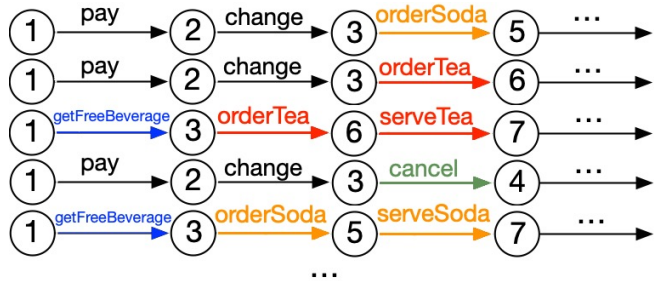


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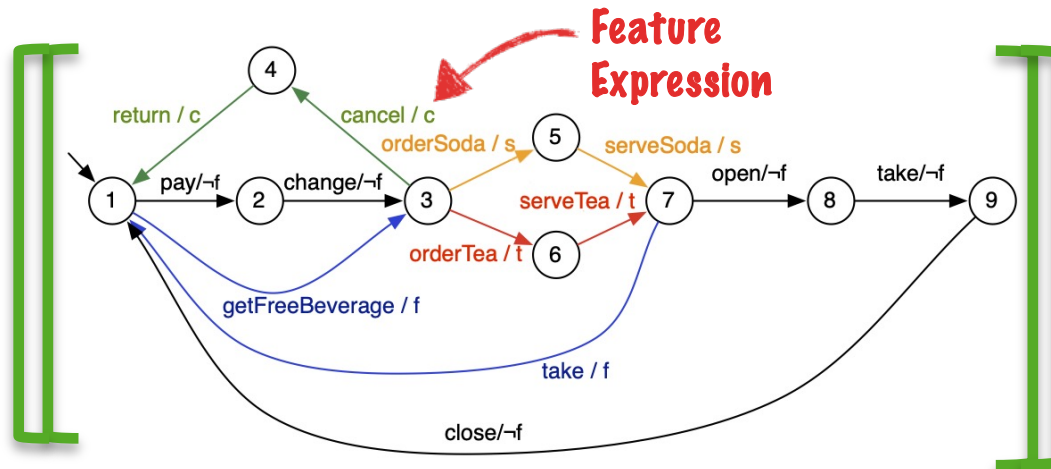


Static Variability:  
Feature Model (FM)

Variability-Aware Behaviour:  
Featured Transition System (FTS)

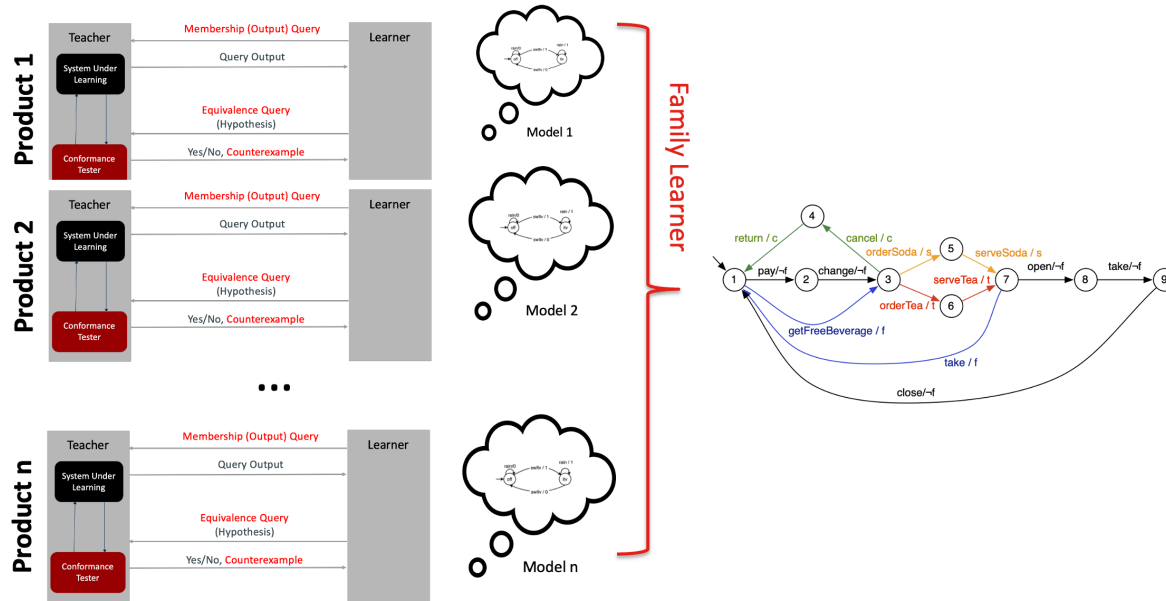


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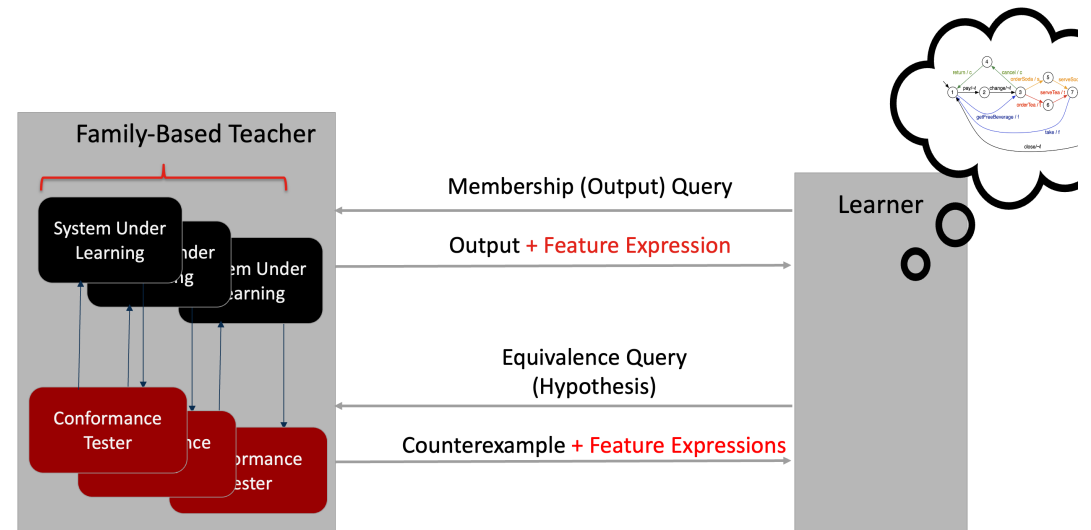
# What?

## Variability-Aware Learner



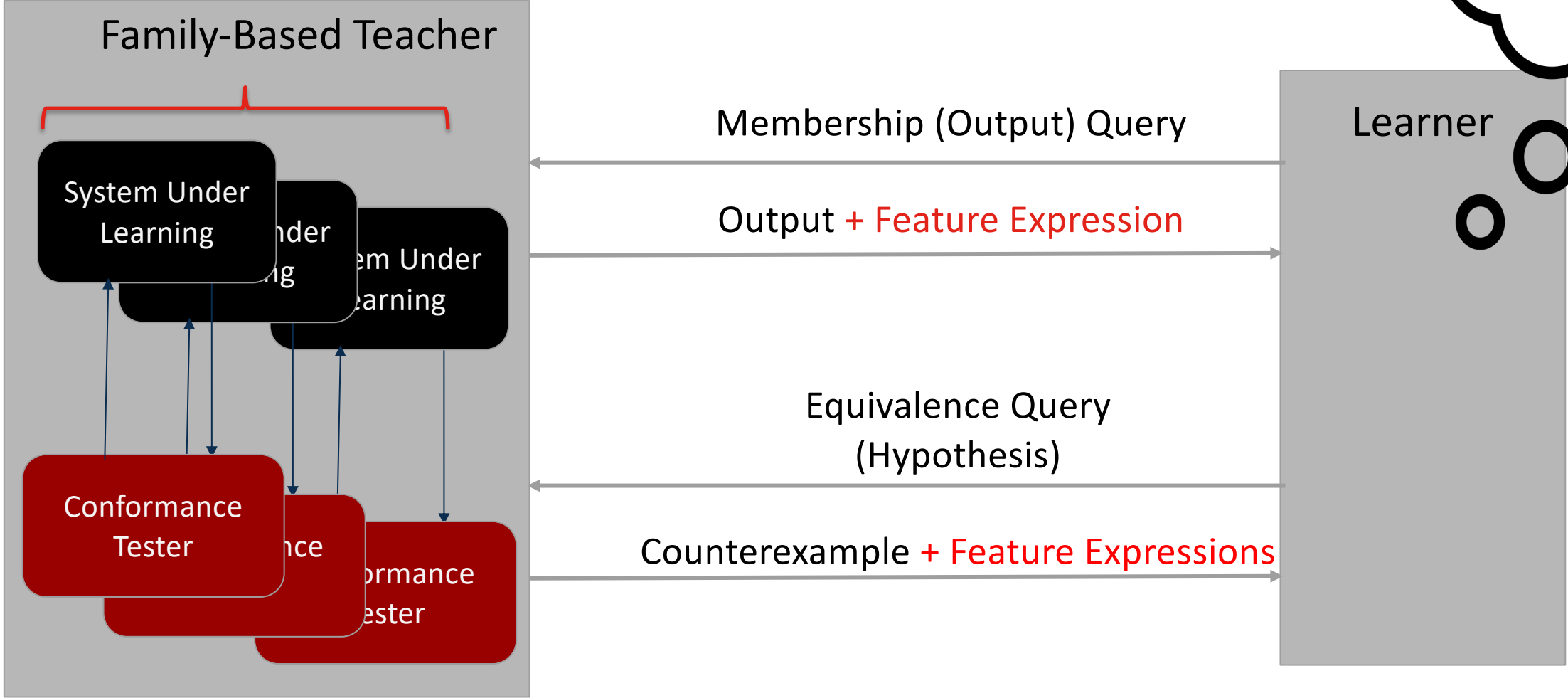
[Damasceno, Mousavi, Simao. Learning by Sampling: Learning Behavioral Family Models from Software Product Lines. EMSE 21]  
 [Tavassoli, Damasceno, Khosravi, Mousavi, Adaptive Behavioral Model Learning for Software Product Lines. SPLC 2022]

## Variability-Aware Teacher

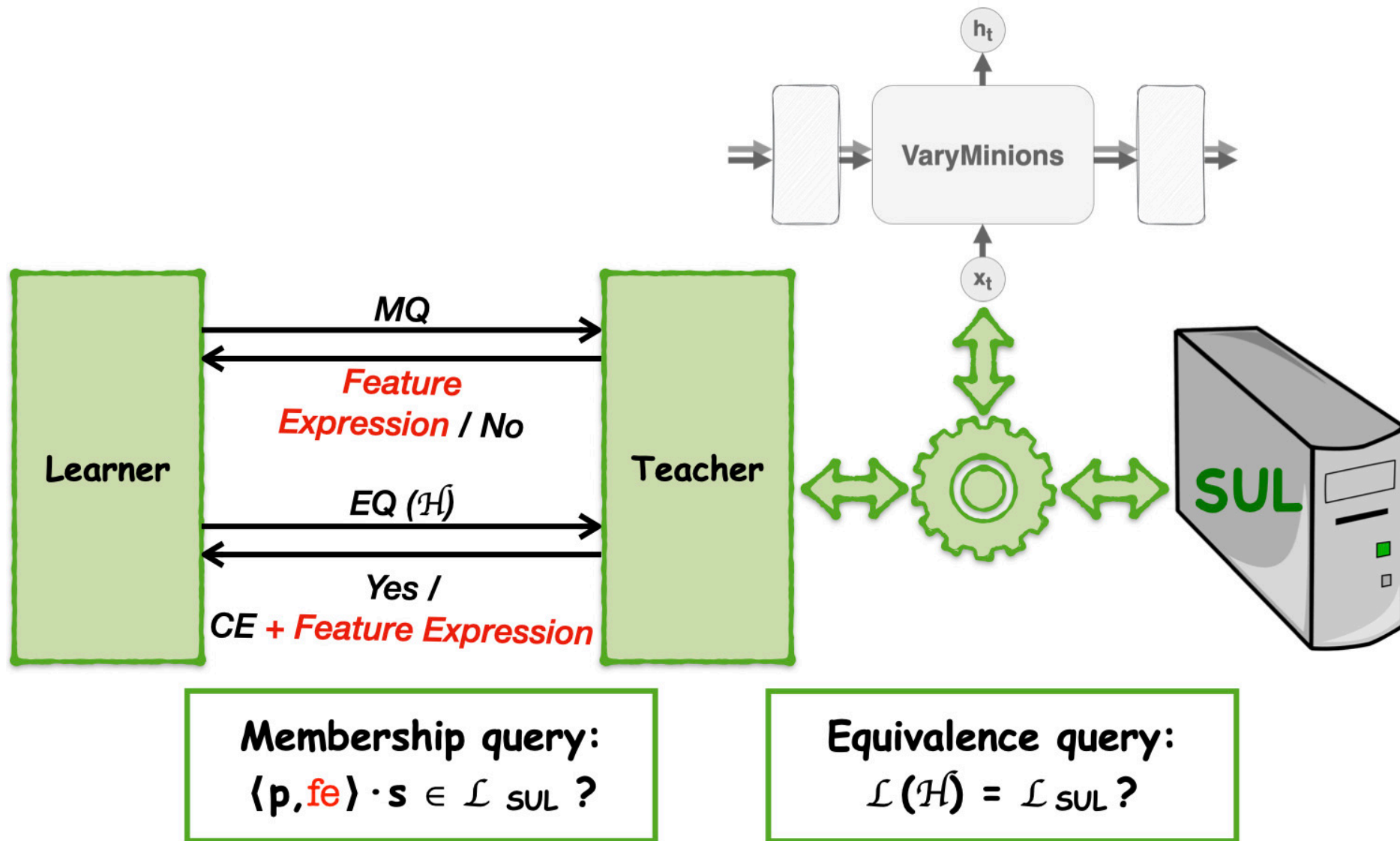


[Fortz, Temple, Devroey, Heymans, Perrouin. VaryMinions: Leveraging RNNs to Identify Variants in Event Logs. MalTeSQuE'21]  
 [Fortz. Variability-aware Behavioural Learning. SPLC Doctoral Symposium'23]  
 [Fortz. LIFTS: learning featured transition systems. SPLC Doctoral Symposium'21]

# Variability-Aware Teacher



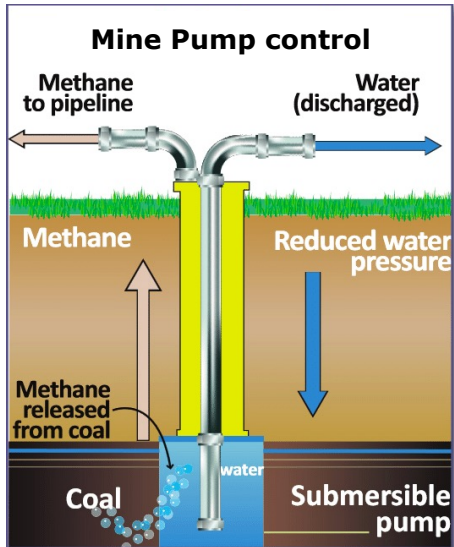
# Featured-L\* (FL\*)



# Case Studies



Model	Features	Products	States	Transitions	Actions
Forum	5	6	5	5	5
SVM	9	24	9	13	13
Minepump	9	32	25	41	24
CP Terminal	21	4.774	11	17	16
Sferion™	25	64	525	46	12



# Evaluation Metrics

## **RQ<sub>1</sub>** How to automatically learn Featured Transition Systems?

- **RQ<sub>1.1</sub>** Time
- **RQ<sub>1.2</sub>** Number of membership queries
- **RQ<sub>1.3</sub>** Number of equivalence queries and learning rounds
- **RQ<sub>1.4</sub>** Number of resets

# Results

Model	Time	MQ	EQ	Rounds	Resets
<b>Forum</b>	1 s.	546	7	3	15.596
<b>SVM</b>	9 s.	19.836	23	6	219.430
<b>Minepump</b>	9 m.	186.984	54	11	2,934,811
<b>CP Terminal</b>	17 m.	39.780	33	9	436.942
<b>Sferion™</b>	117 m.	72.803	363	6	57,057,295

# Contributions

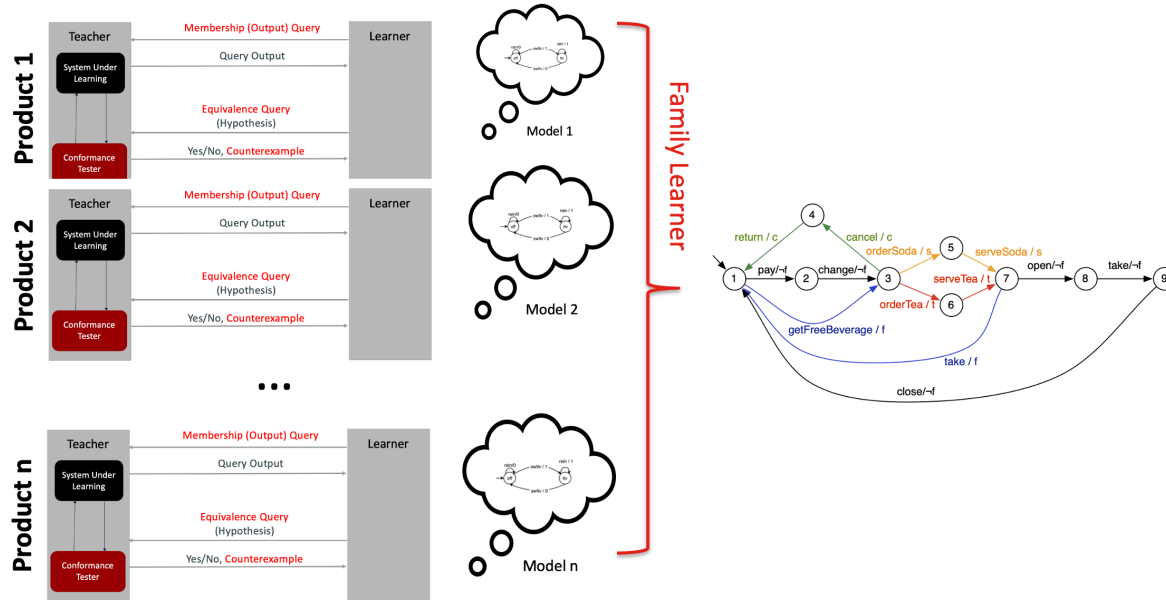
- FE as first-class citizen
- Direct mapping on transitions
- Fully family-based approach

- Observation table of 8,904 prefixes X 21 suffixes (Minepump)
- Up to 129 states and 356 transitions (Sferion™)
- After simplification:
  - 77 % to 98 % of reduction for the observation table
  - up to 80 % of reduction for the automaton (Minepump)
- Less than 2 hours of execution for each study ( 2 Cores, 2 Sockets, 16Go RAM)



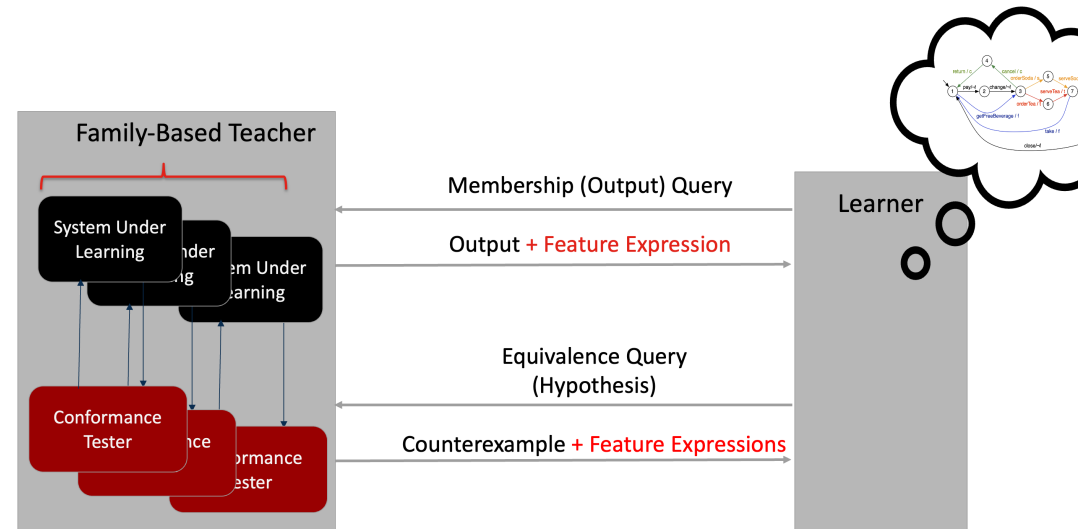
# What?

## Variability-Aware Learner



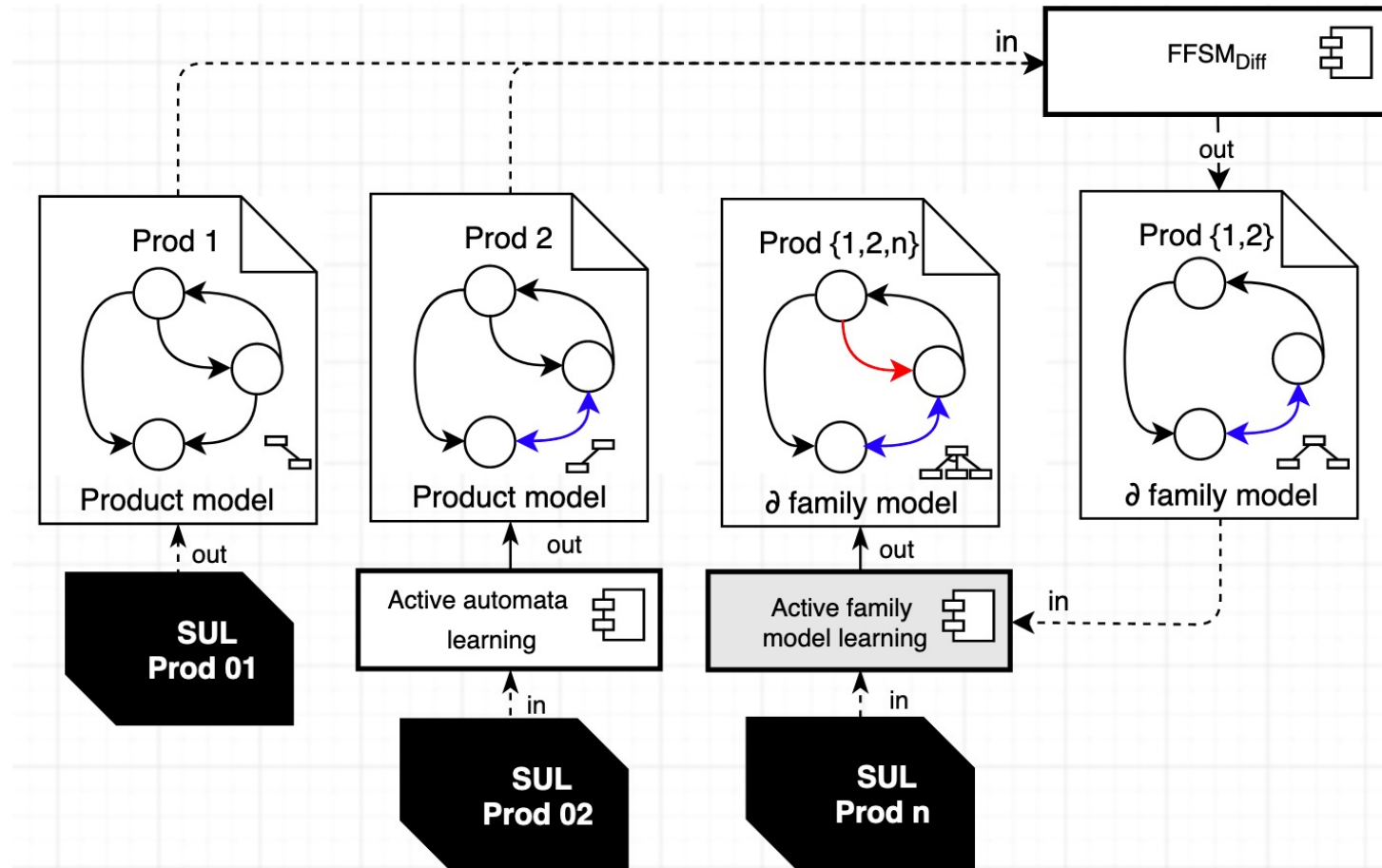
[Damasceno, Mousavi, Simao. Learning by Sampling: Learning Behavioral Family Models from Software Product Lines. EMSE 21]  
 [Tavassoli, Damasceno, Khosravi, Mousavi, Adaptive Behavioral Model Learning for Software Product Lines. SPLC 2022]

## Variability-Aware Teacher



[Fortz, Temple, Devroey, Heymans, Perrouin. VaryMinions: Leveraging RNNs to Identify Variants in Event Logs. MalTeSQuE'21]  
 [Fortz. SPLC Doctoral Symposium'21 and '23]

# What?



[Damasceno, Mousavi, Simao.]

Learning by Sampling: Learning Behavioral Family Models from Software Product Lines. EMSE 21]

# How?

$$S_{Succ}^G(a, b) = \frac{1}{2} \frac{\sum_{(c,d,i,o) \in Succ_{a,b}} (1 + k \times S_{Succ}^G(c, d))}{|\sum_r^{out}(a) - \sum_u^{out}(b)| + |\sum_r^{out}(b) - \sum_u^{out}(a)| + |Succ_{a,b}|}$$

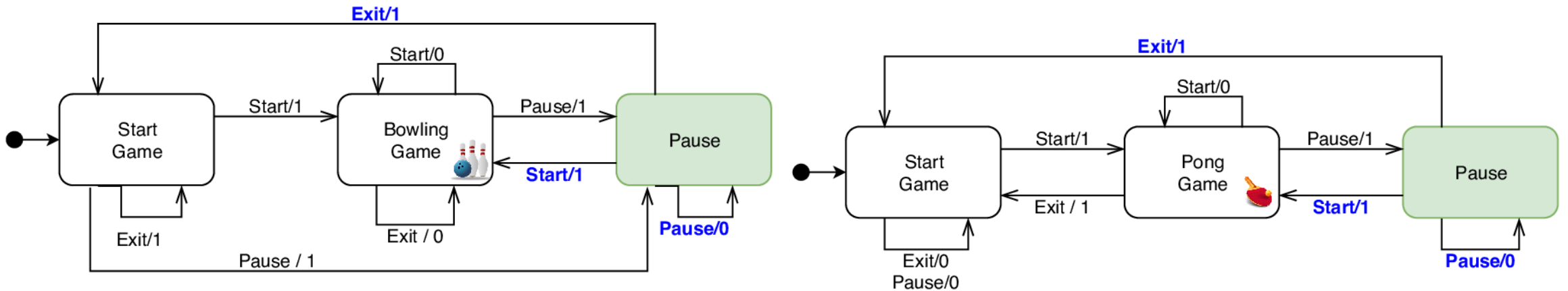
## Global similarity score (Outgoing and incoming transitions)

- Pairwise similarity based on surrounding matching transitions and connected state pairs.
- Attenuation ratio  $k$  gives precedence to the closest state pairs.
- **Matching transitions** and distinct transitions.

[N. Walkinshaw and K. Bogdanov,  
Automated Comparison of State-Based Software Models  
in Terms of Their Language and Structure.]

# How?

$$S_{Succ}^G(Pa, Pa) = \frac{1}{2} \times \frac{3 + k \times [S_{Succ}^G(St, St) + S_{Succ}^G(Bo, Po) + S_{Succ}^G(Pa, Pa)]}{0 + 0 + 3} = 0.58$$



# The FFSM<sub>Diff</sub> algorithm

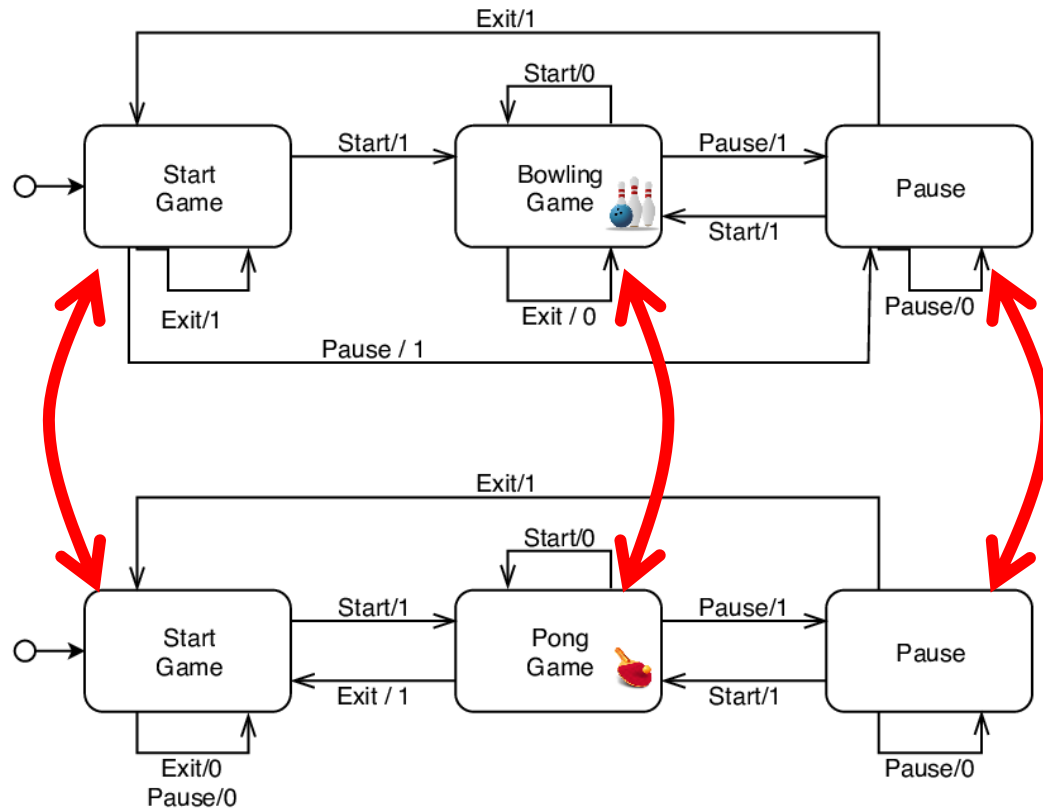


Figure: Two examples of product FSMs

$$\text{pair}(St, St) = 0.12$$

$$\text{pair}(St, Po) = 0.29$$

$$\text{pair}(St, Pa) = 0.28$$

$$\text{pair}(Bo, St) = 0.11$$

$$\text{pair}(Bo, Po) = 0.31$$

$$\text{pair}(Bo, Pa) = 0$$

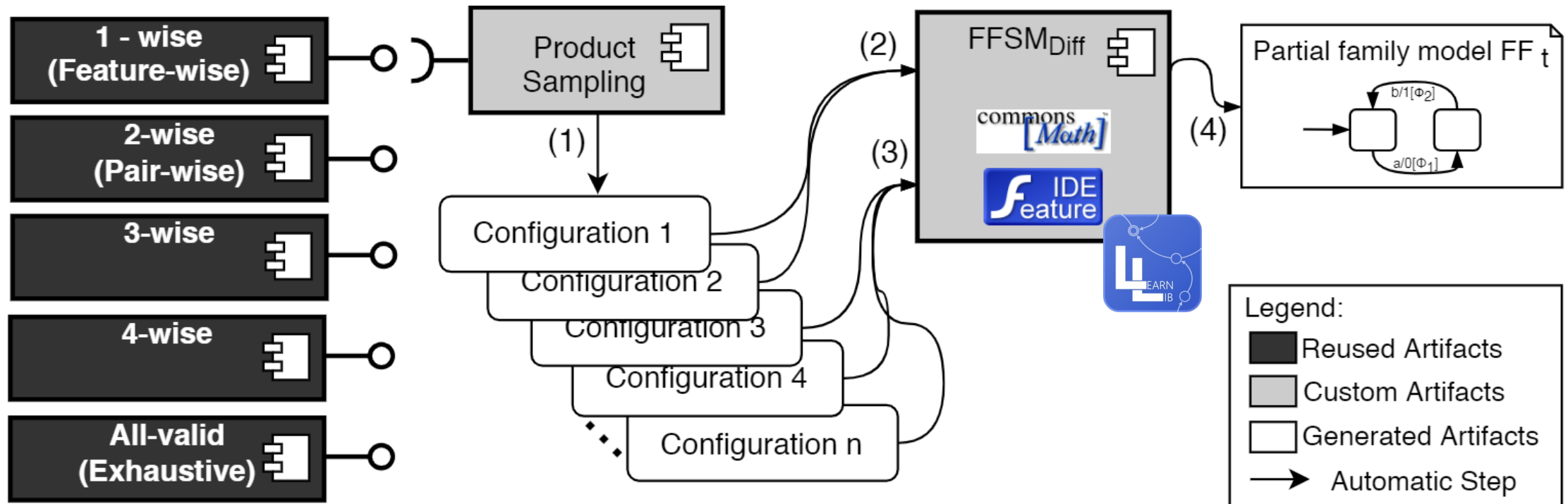
$$\text{pair}(Pa, St) = 0.29$$

$$\text{pair}(Pa, Po) = 0.11$$

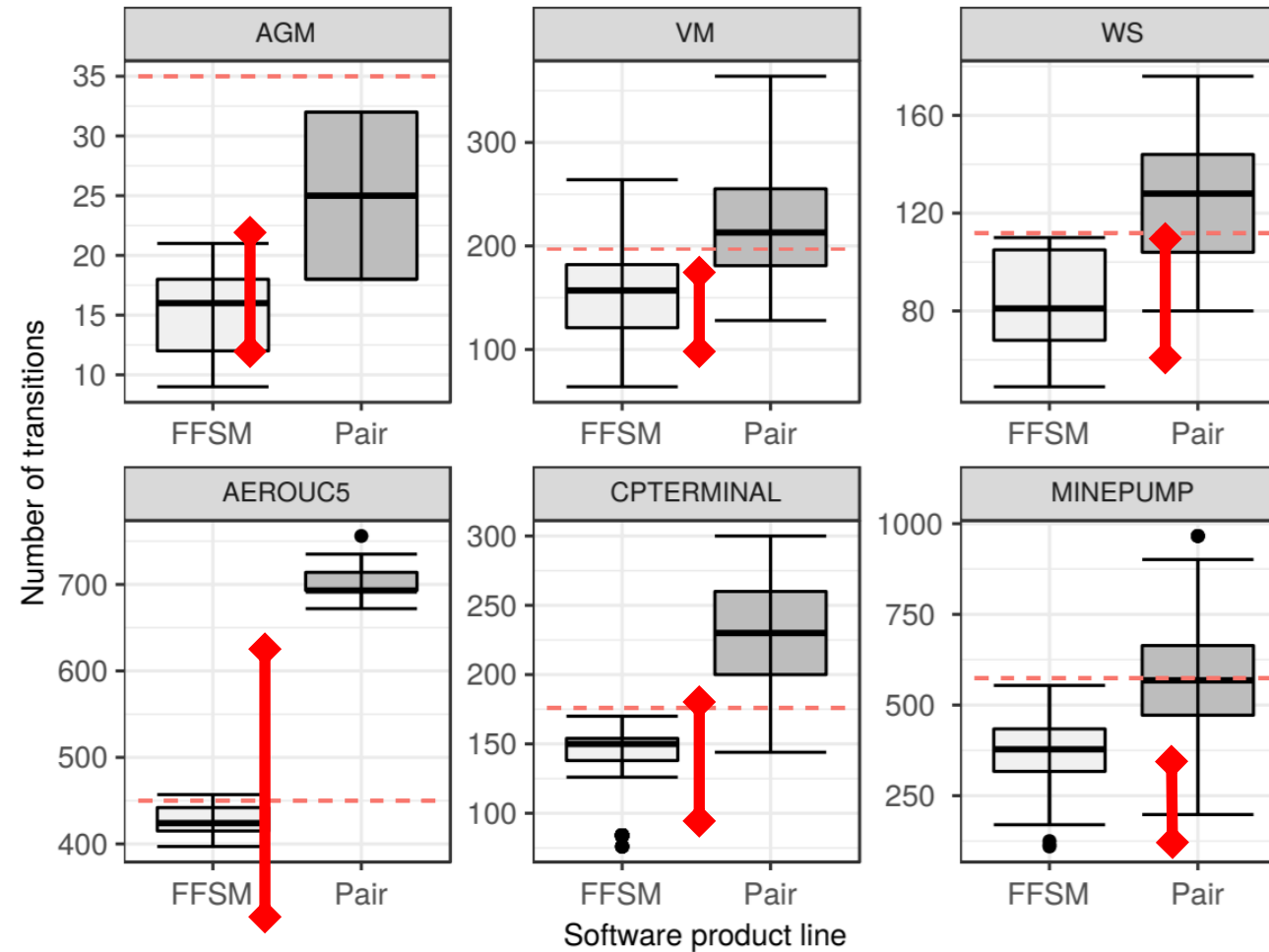
$$\text{pair}(Pa, Pa) = 0.58$$

Figure: Pairwise state similarity

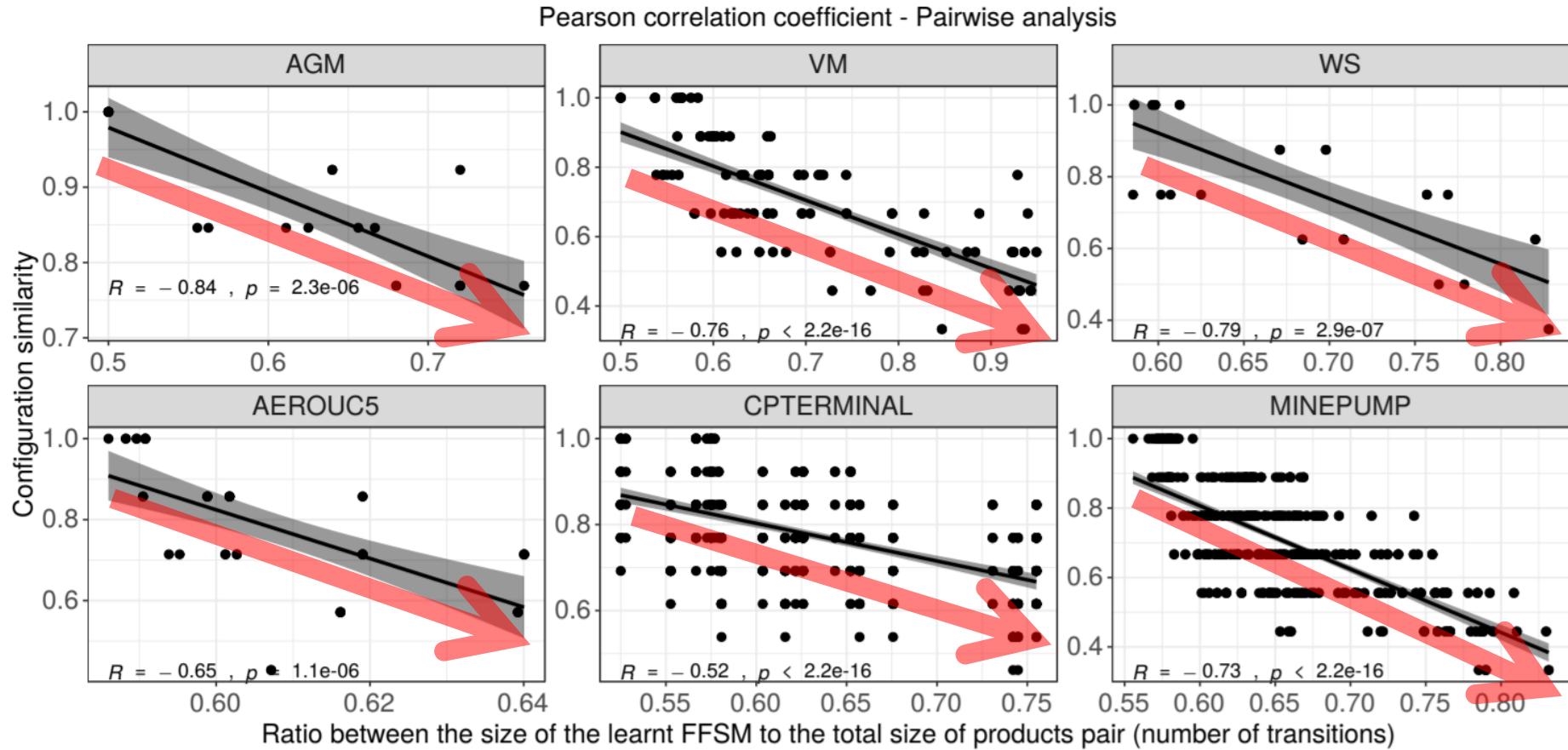
# Experiment Design



# Analysis of Results: Size

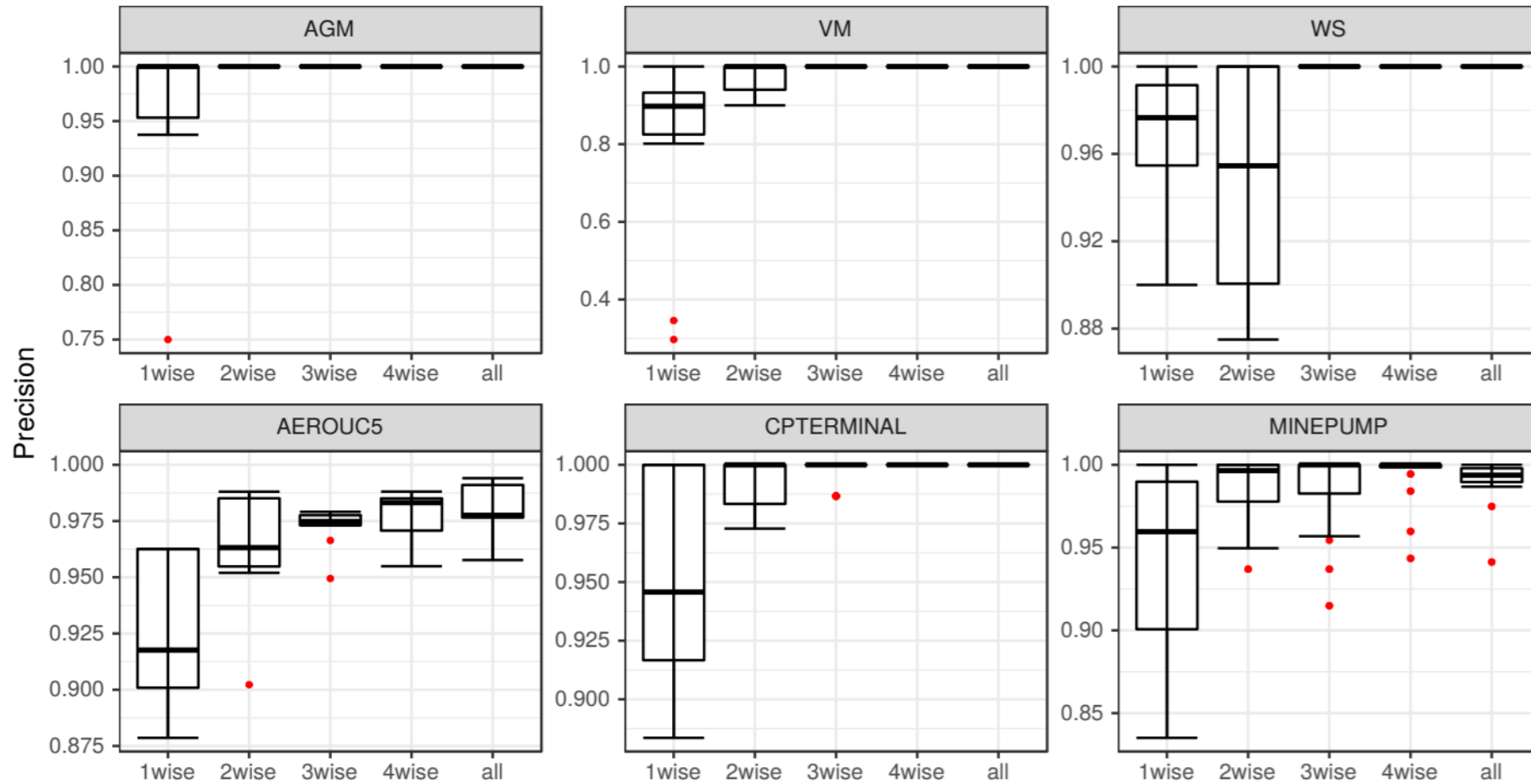


# Analysis of Results





# Analysis of Results: Sampling



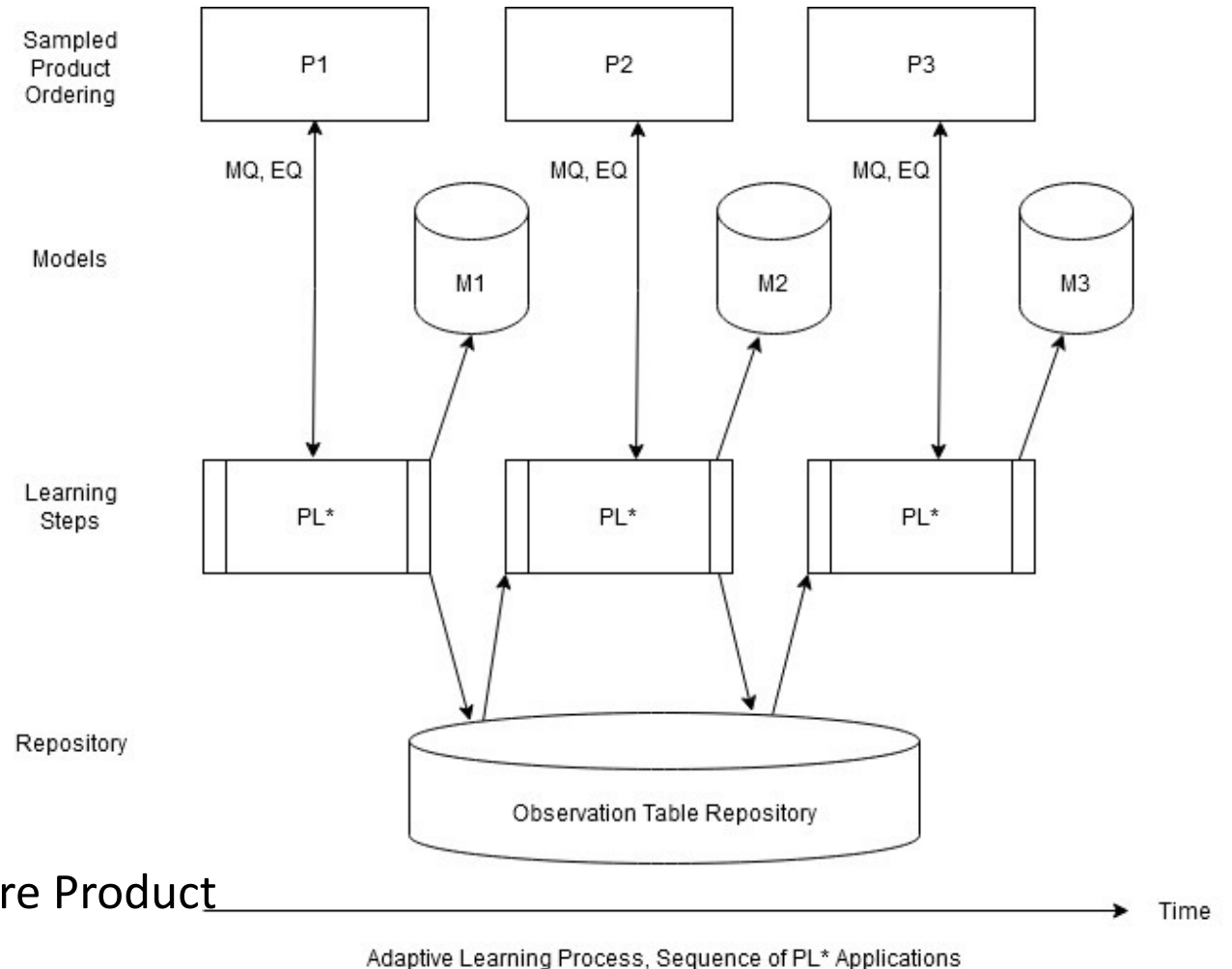
More precise family models

Higher values of T

[Damasceno, Mousavi, Simao.  
Learning by Sampling: Learning Behavioral Family Models from  
Software Product Lines. EMSE 21]

# PL\*

## Building a repository of queries that for changes in space



[Tavassoli, Damasceno, Khosravi, Mousavi, Adaptive Behavioral Model Learning for Software Product Lines. SPLC 2022]



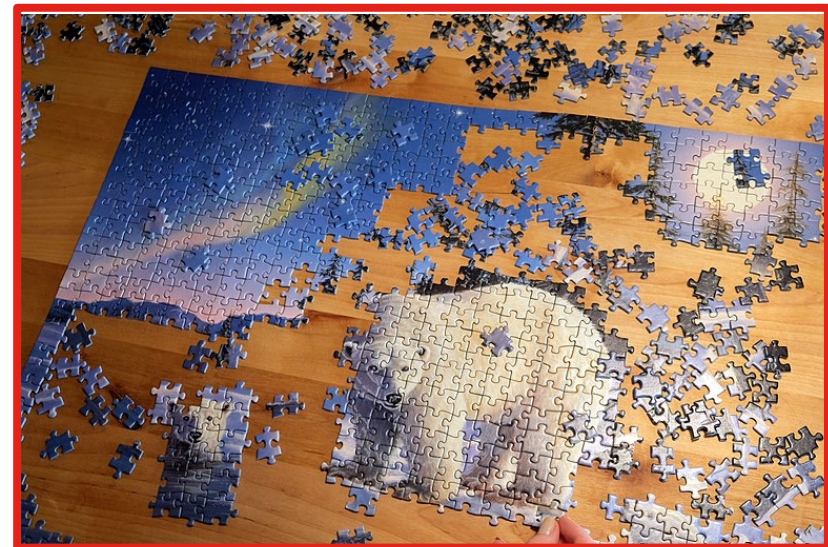
**Active Automata Learning**



**Adaptive Learning**

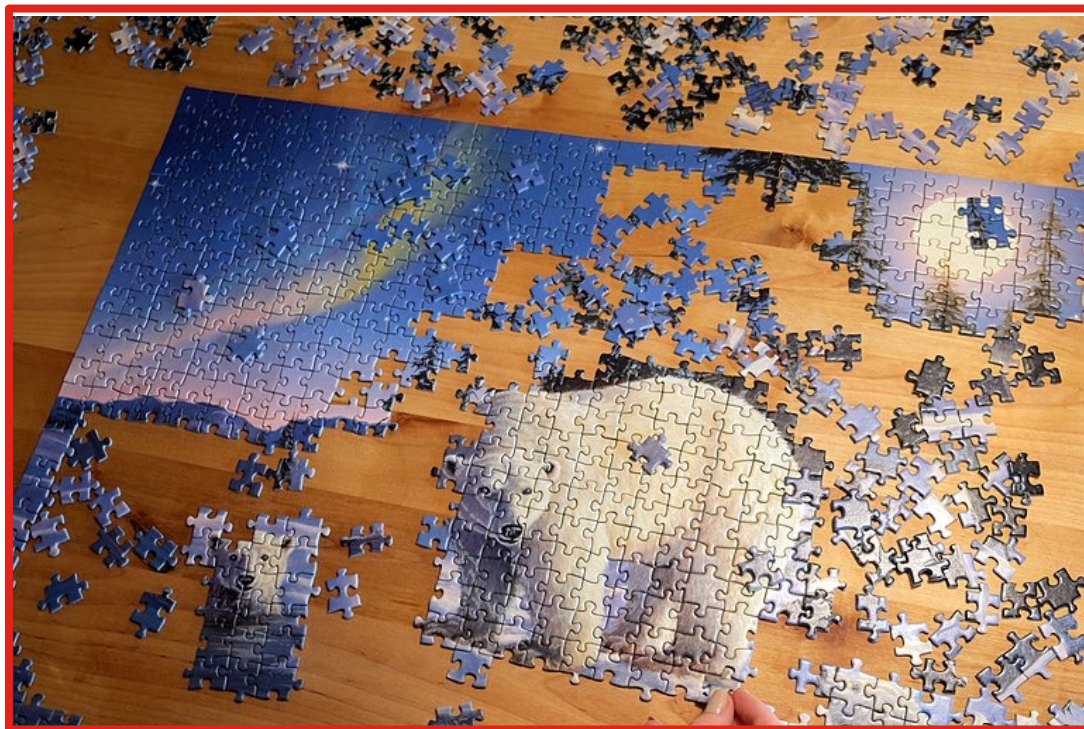


**Produc Line Learning**

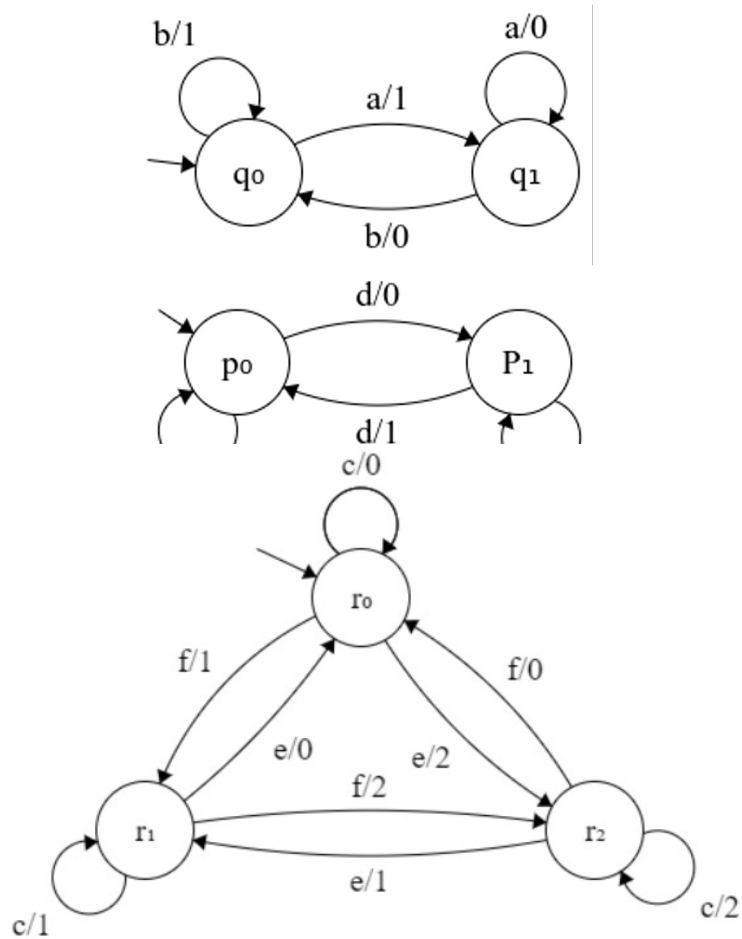


**Compositional Learning**

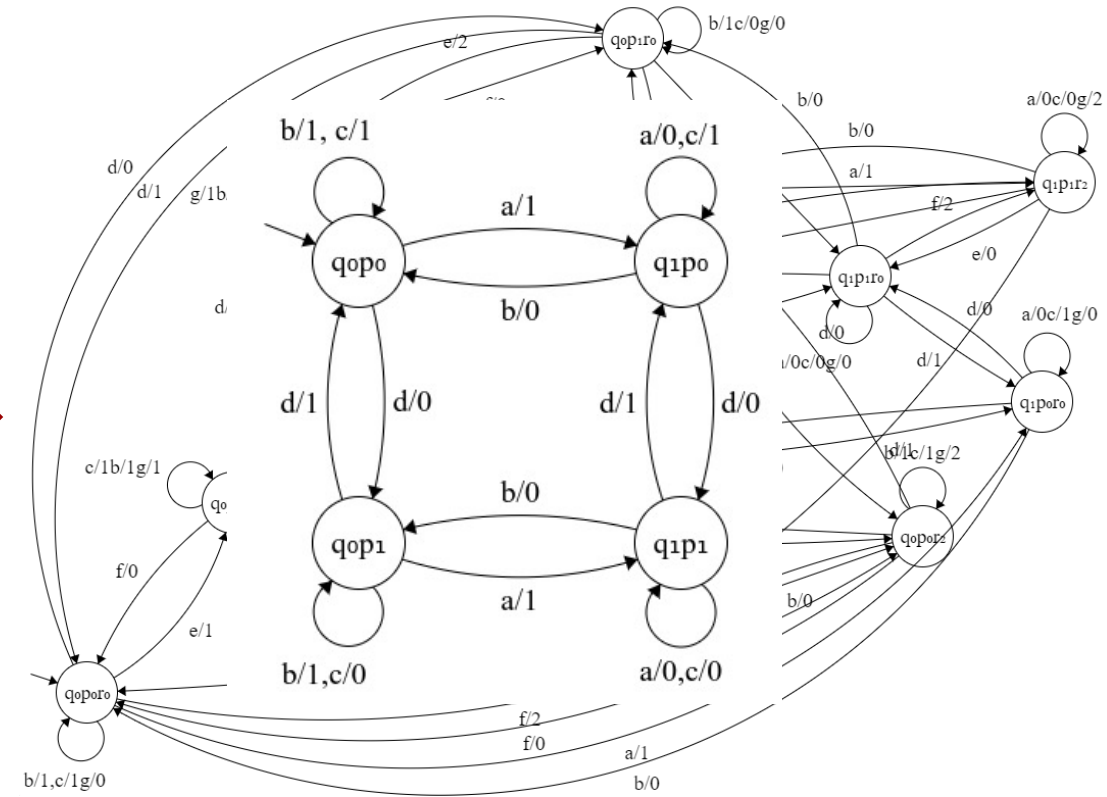
# Compositional Learning

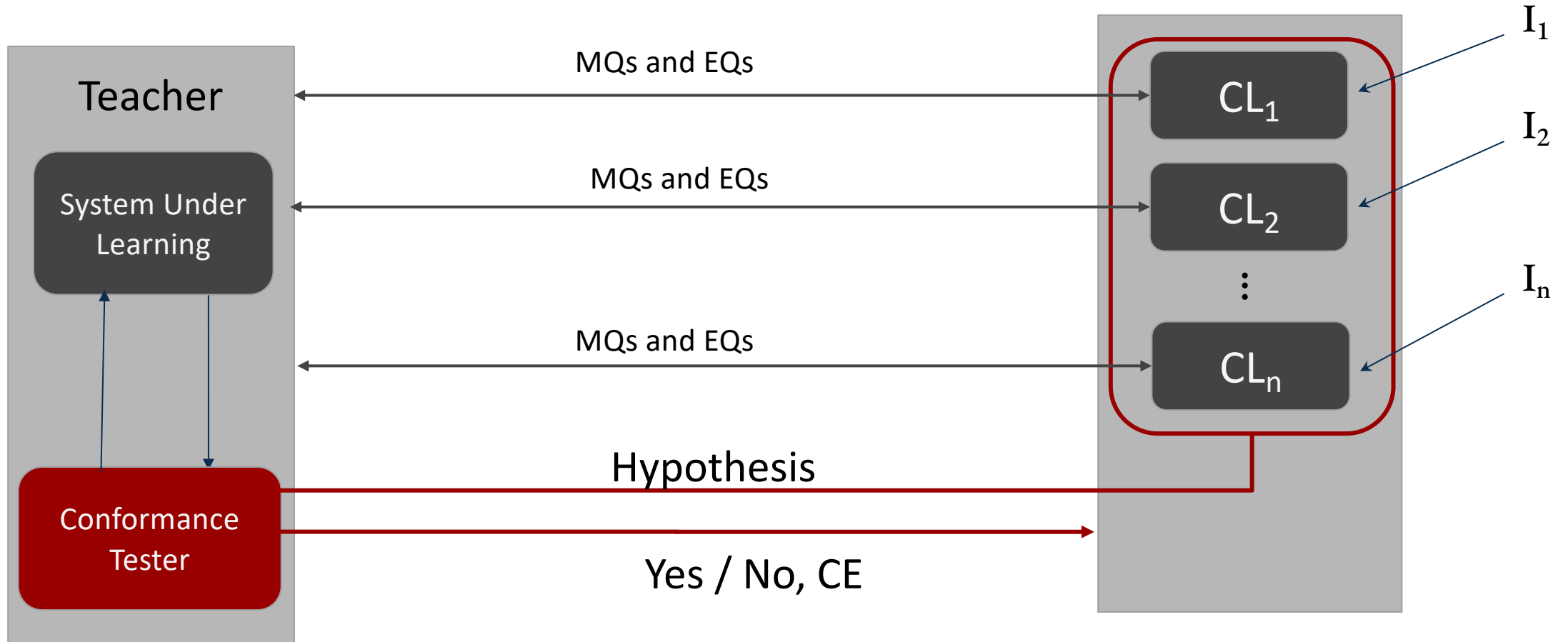


# Interleaving Parallel Systems

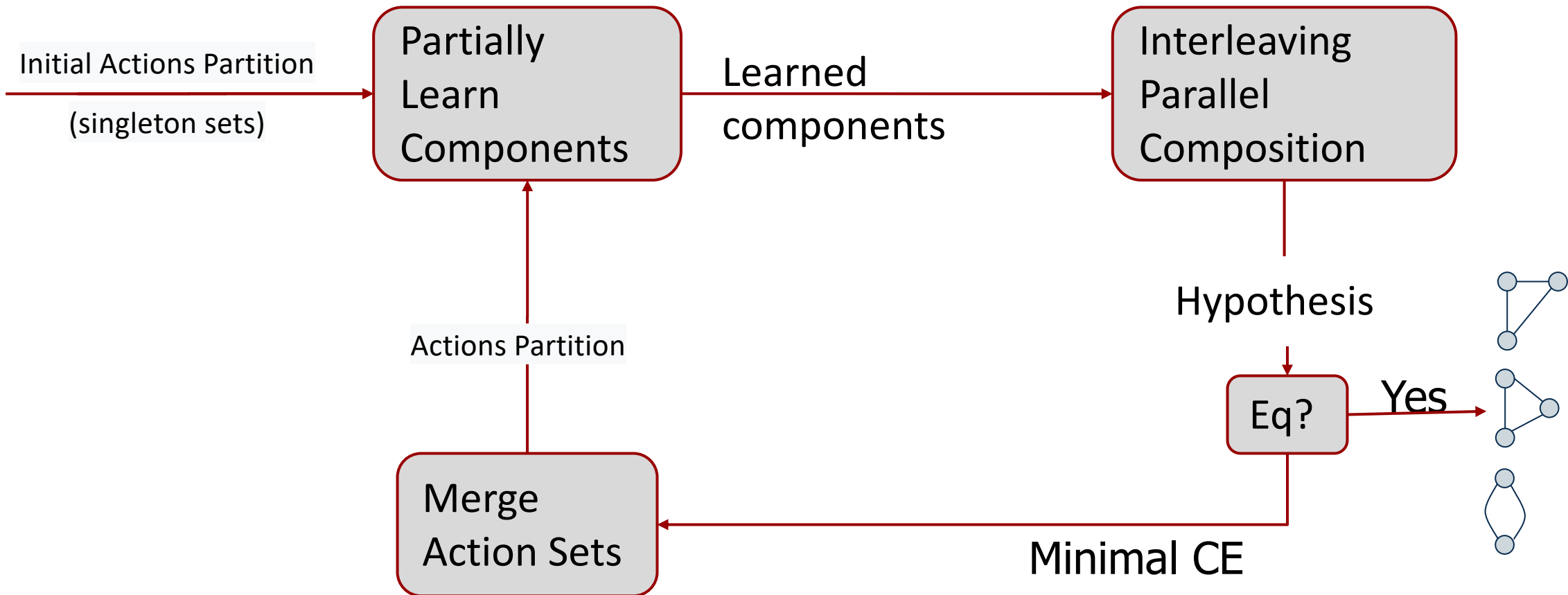


Interleaving Parallel Composition

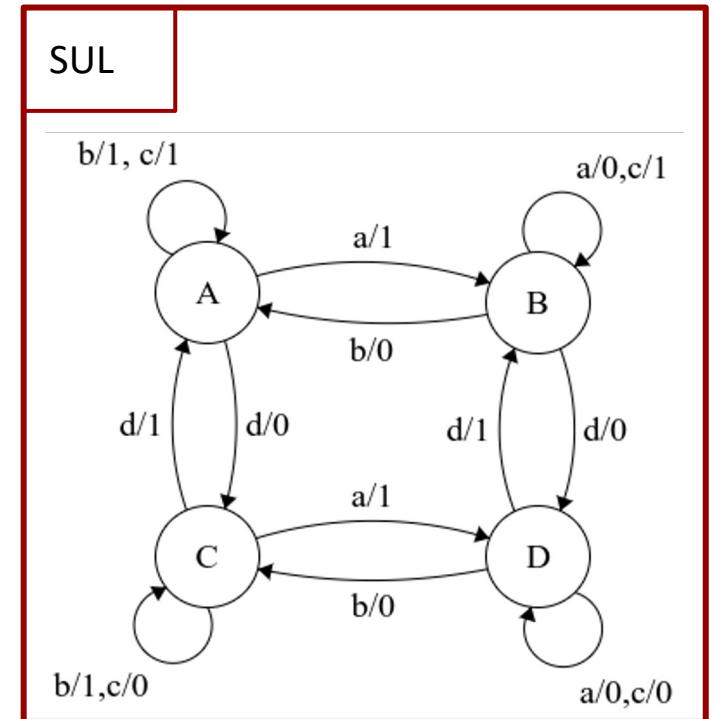
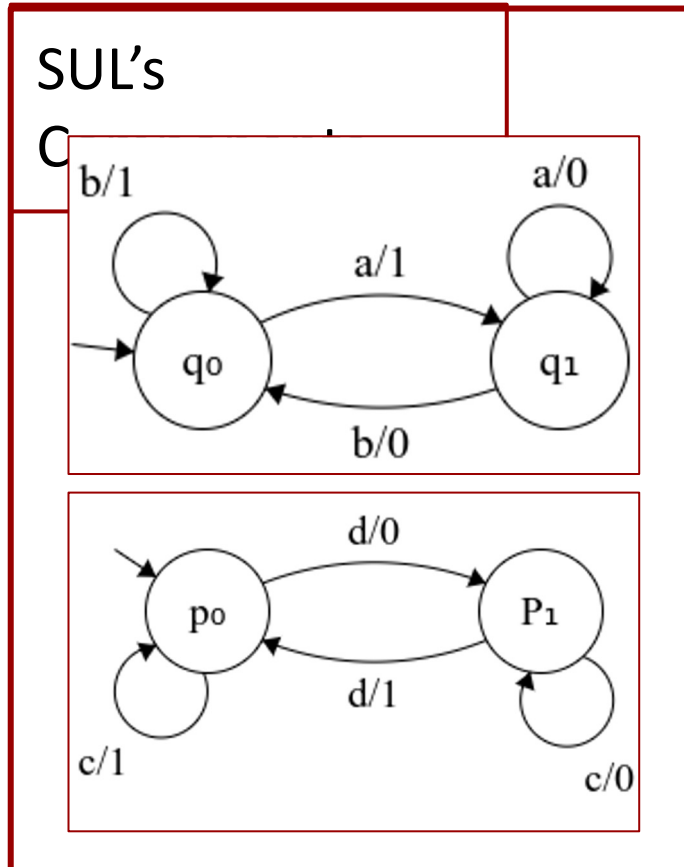




# CL\* Algorithm



# CL\* Algorithm - Example

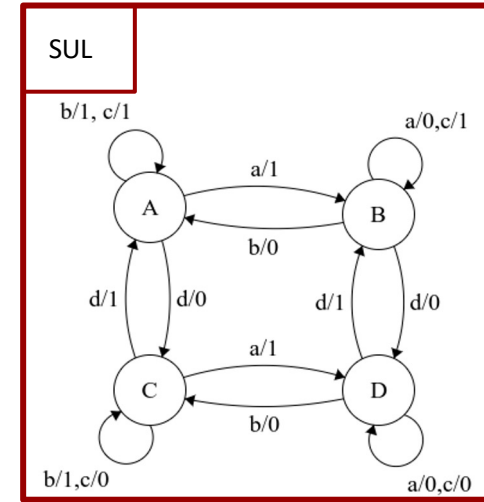
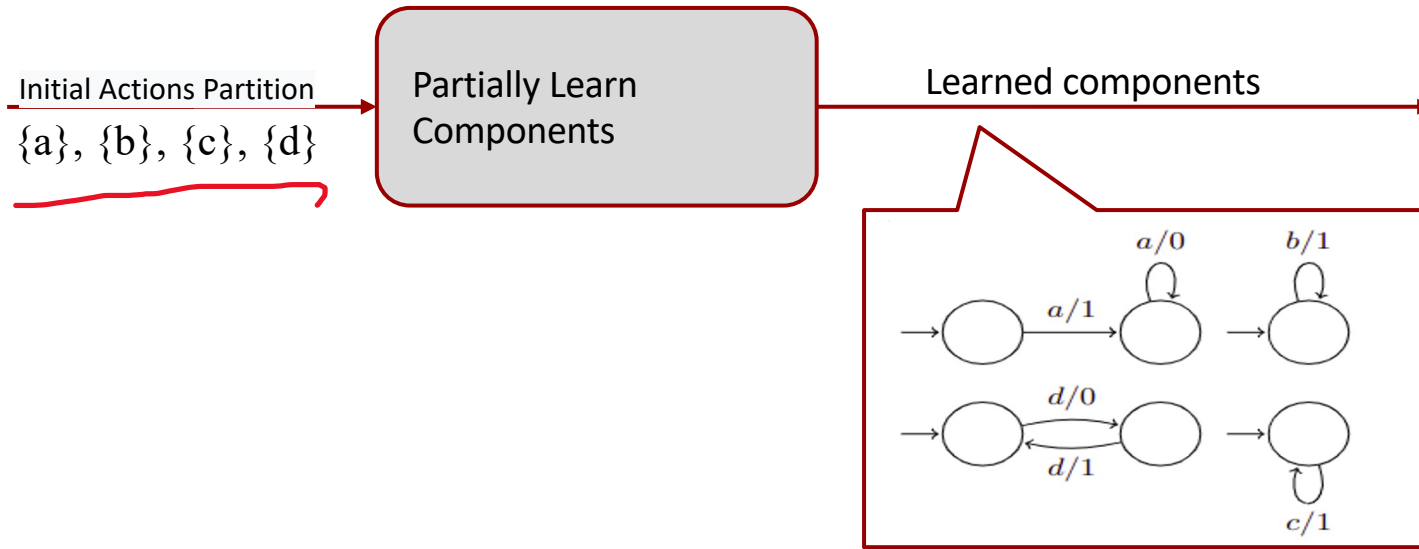


$$I = \{a, b, c, d\}$$

$$O = \{0, 1\}$$



# CL\* Algorithm - Example



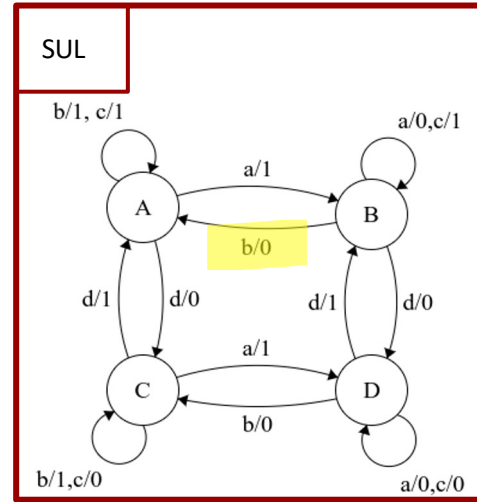
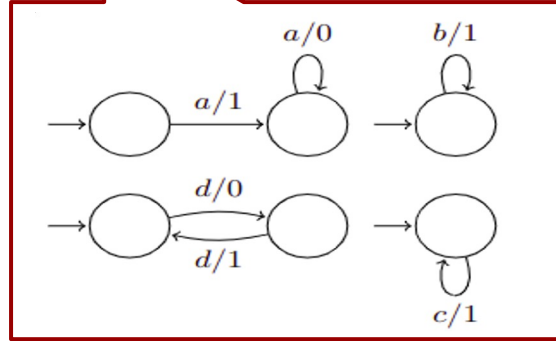
# CL\* Algorithm - Example

Initial Actions Partition  
 $\{a\}, \{b\}, \{c\}, \{d\}$

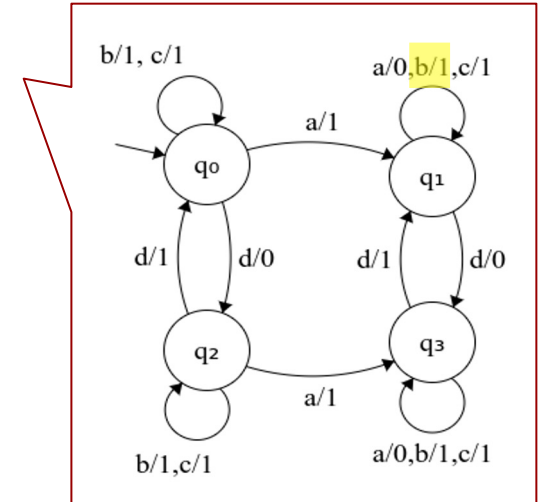
Partially Learn  
 Components

Learned components

Interleaving Parallel  
 Composition



Hypothesis



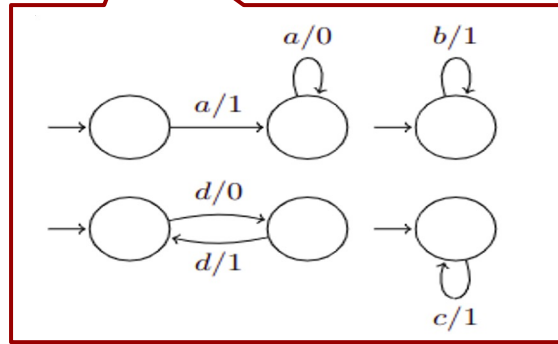
# CL\* Algorithm - Example

Initial Actions Partition  
 $\{a\}, \{b\}, \{c\}, \{d\}$

Partially Learn Components

Learned components

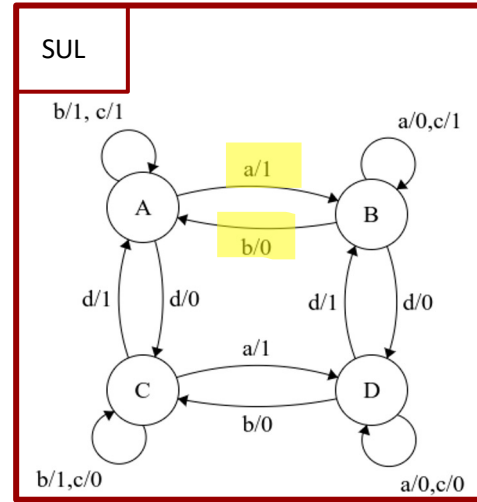
Interleaving Parallel Composition



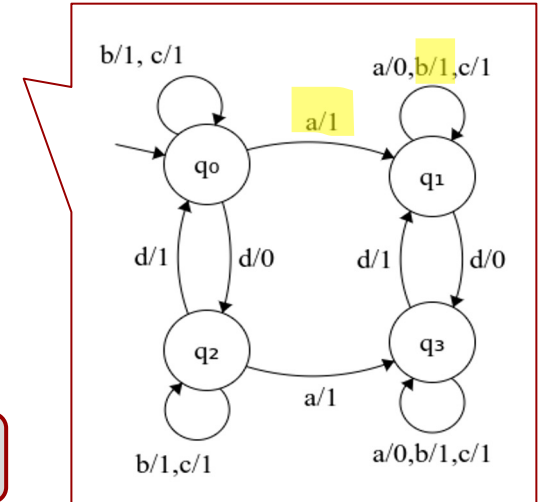
CE = **ab**  
 $M(ab) = 10$   
 $H(ab) = 11$

Eq?

Minimal CE



Hypothesis



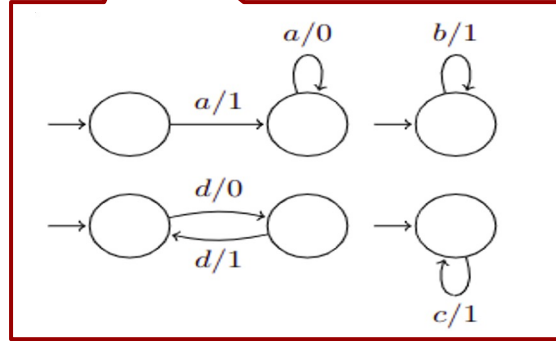
# CL\* Algorithm - Example

Initial Actions Partition  
 $\{a\}, \{b\}, \{c\}, \{d\}$

Partially Learn Components

Learned components

Interleaving Parallel Composition



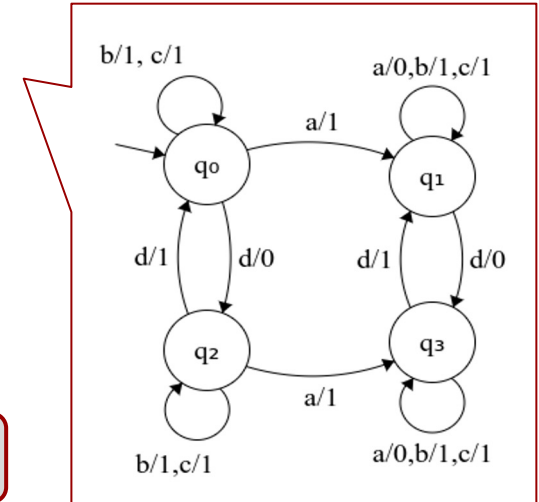
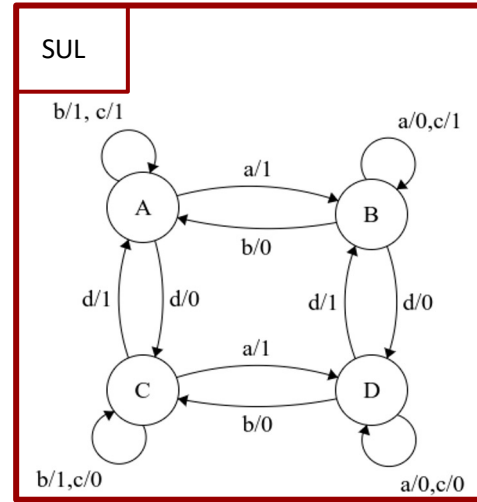
CE = ab  
 $M(ab) = 10$   
 $H(ab) = 11$

Hypothesis

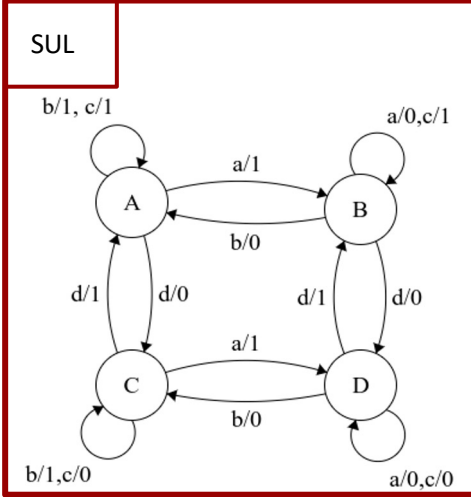
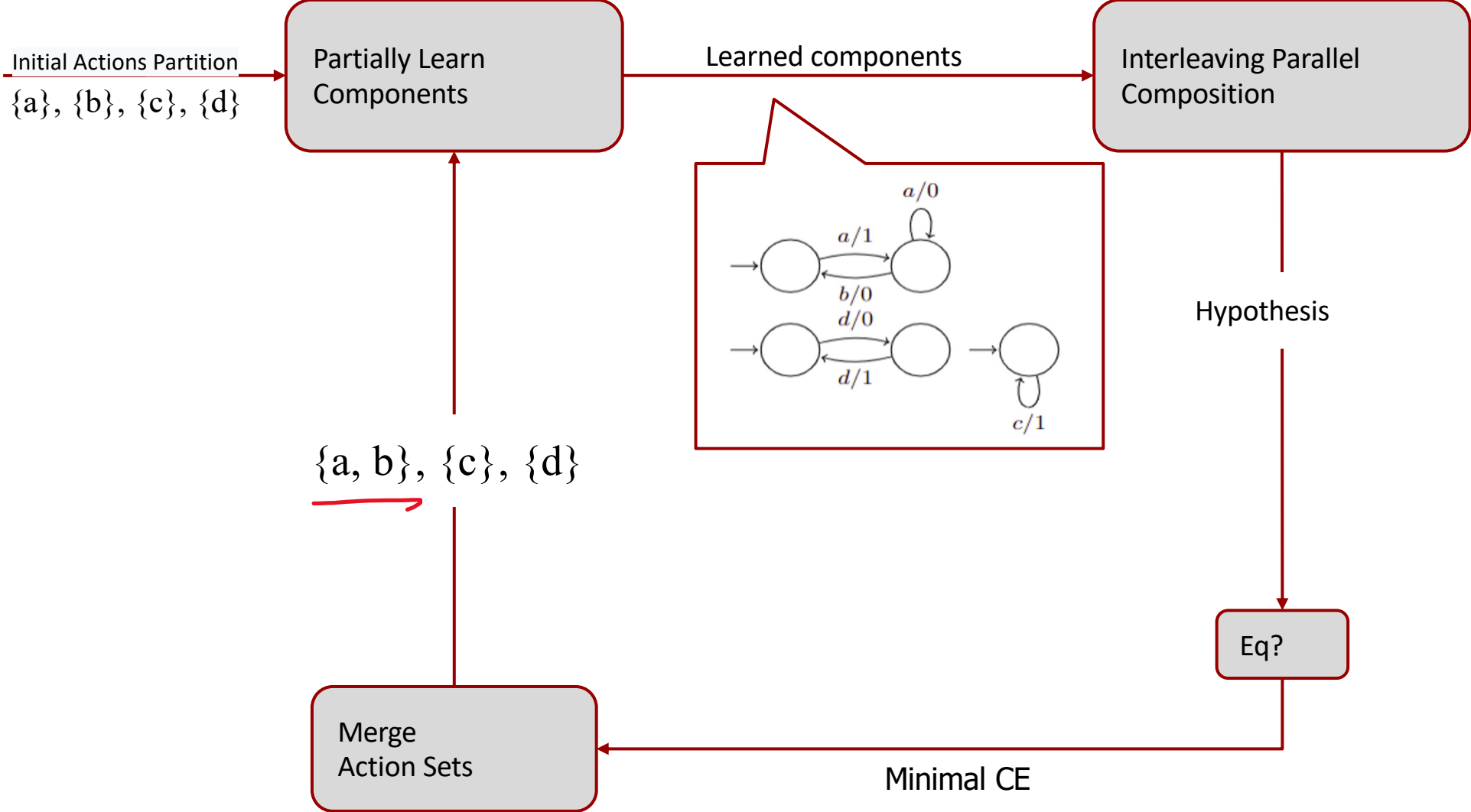
Eq?

Merge Action Sets

Minimal CE



# CL\* Algorithm - Example



# CL\* Algorithm - Example

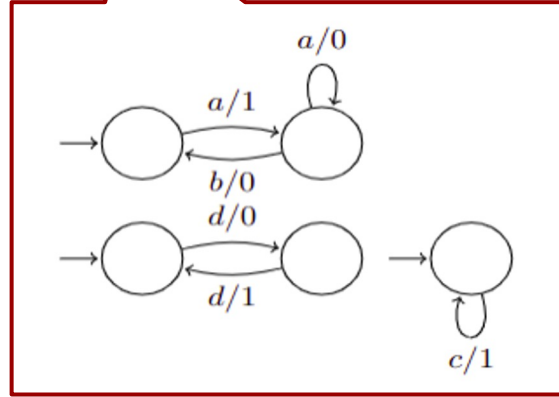
Initial Actions Partition  
 $\{a\}, \{b\}, \{c\}, \{d\}$

Partially Learn  
 Components

Learned components

Interleaving Parallel  
 Composition

$\{a, b\}, \{c\}, \{d\}$



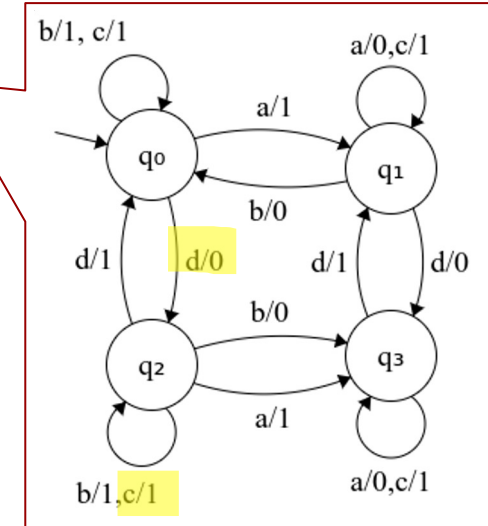
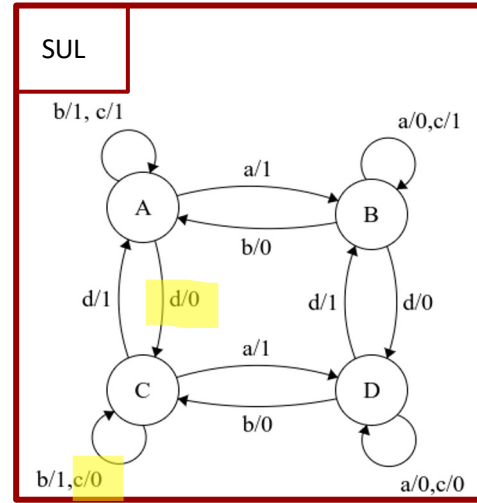
CE = dc  
 M(dc) = 00  
 H(dc) = 01

Hypothesis

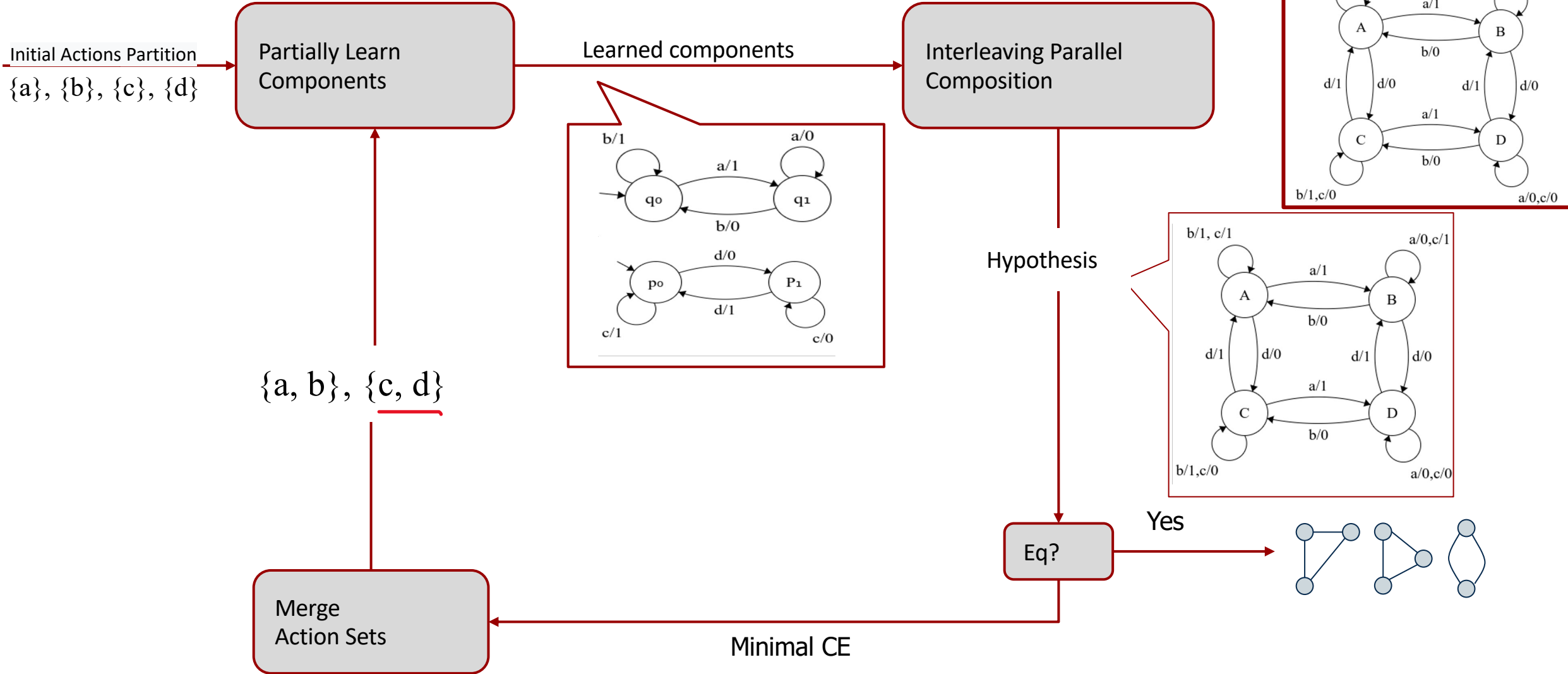
Eq?

Merge  
 Action Sets

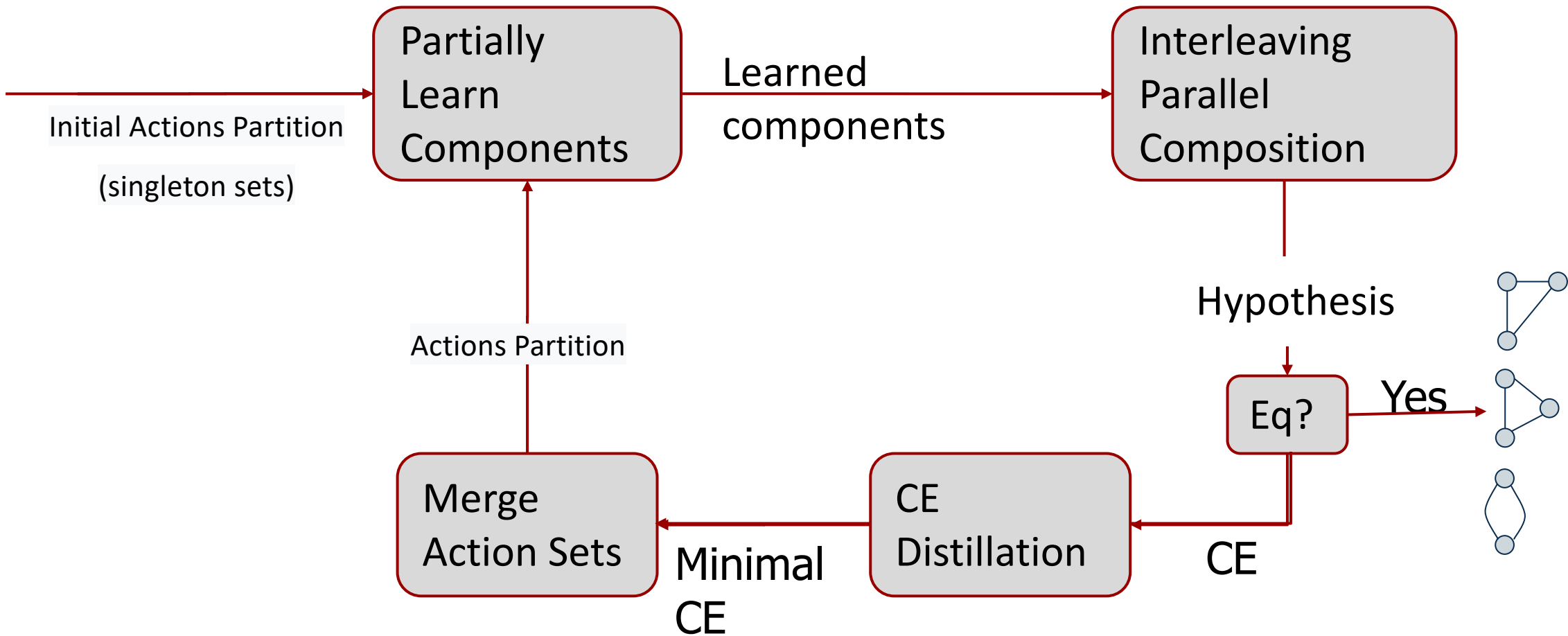
Minimal CE



# CL\* Algorithm - Example



# CL\* Algorithm





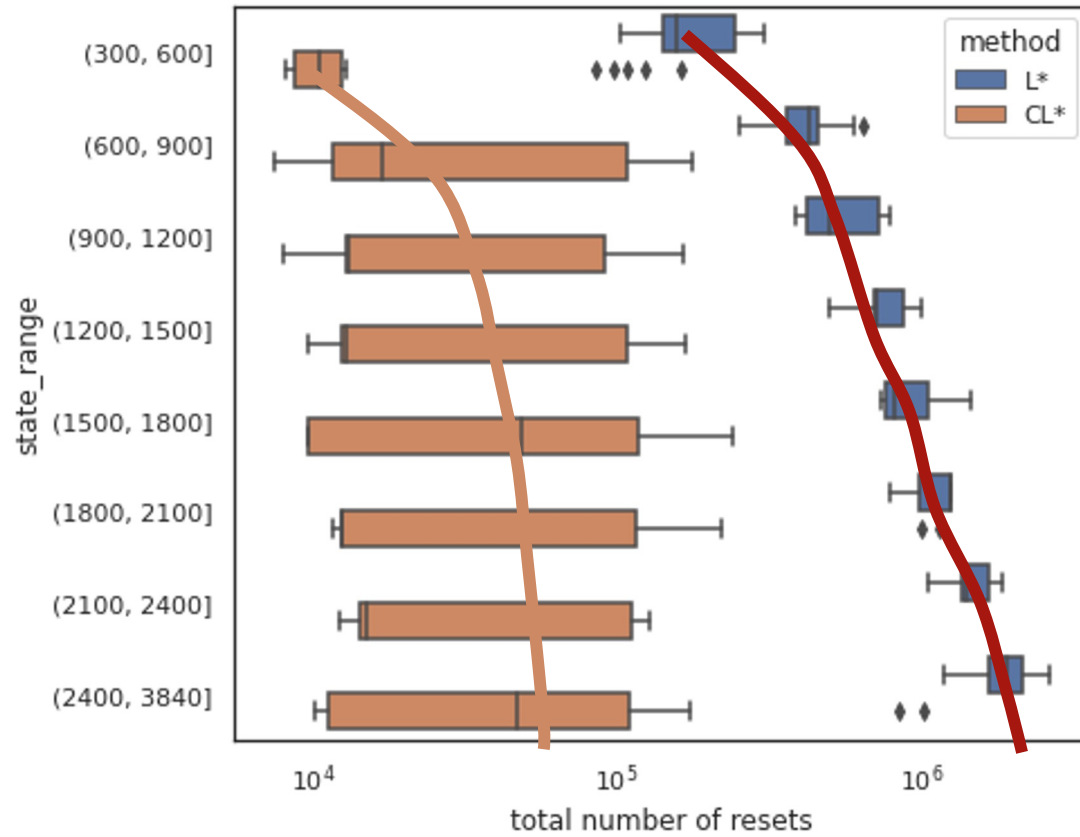
# Experiments: Subject Systems

- Body Comfort System
  - An **automotive software product line** of Volkswagen Golf model.
  - Contains **27 components**
- Benchmarks
  - 100 FSMs
  - 2 to 9 components
  - 0 to 3840 states, average: 1278

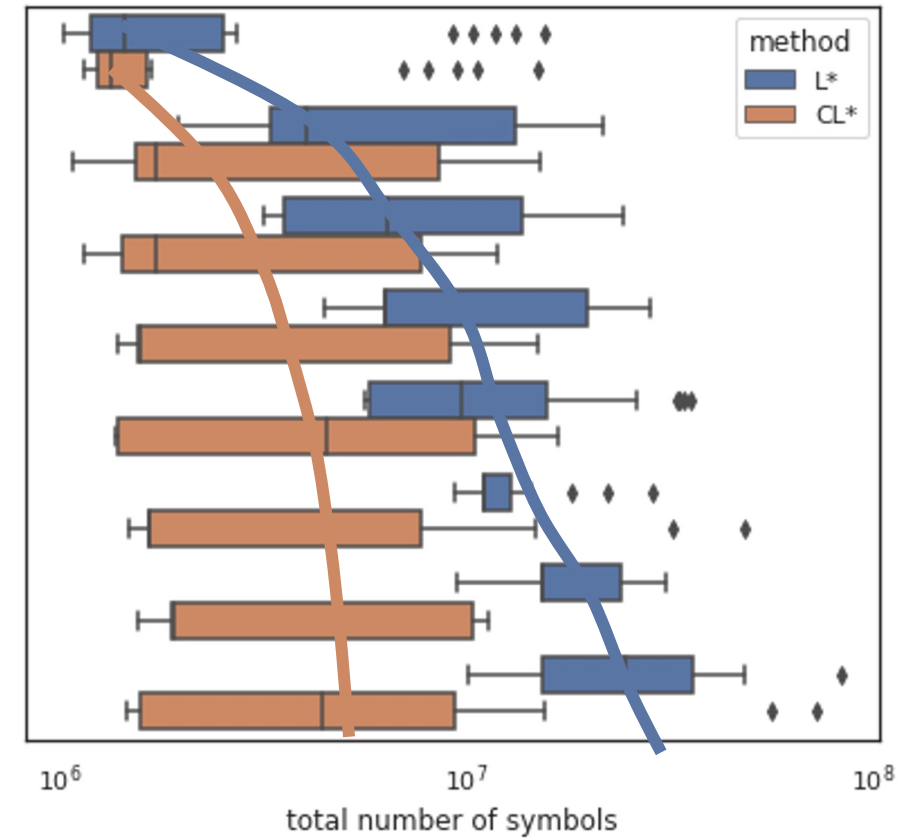


# Experiments: Performance

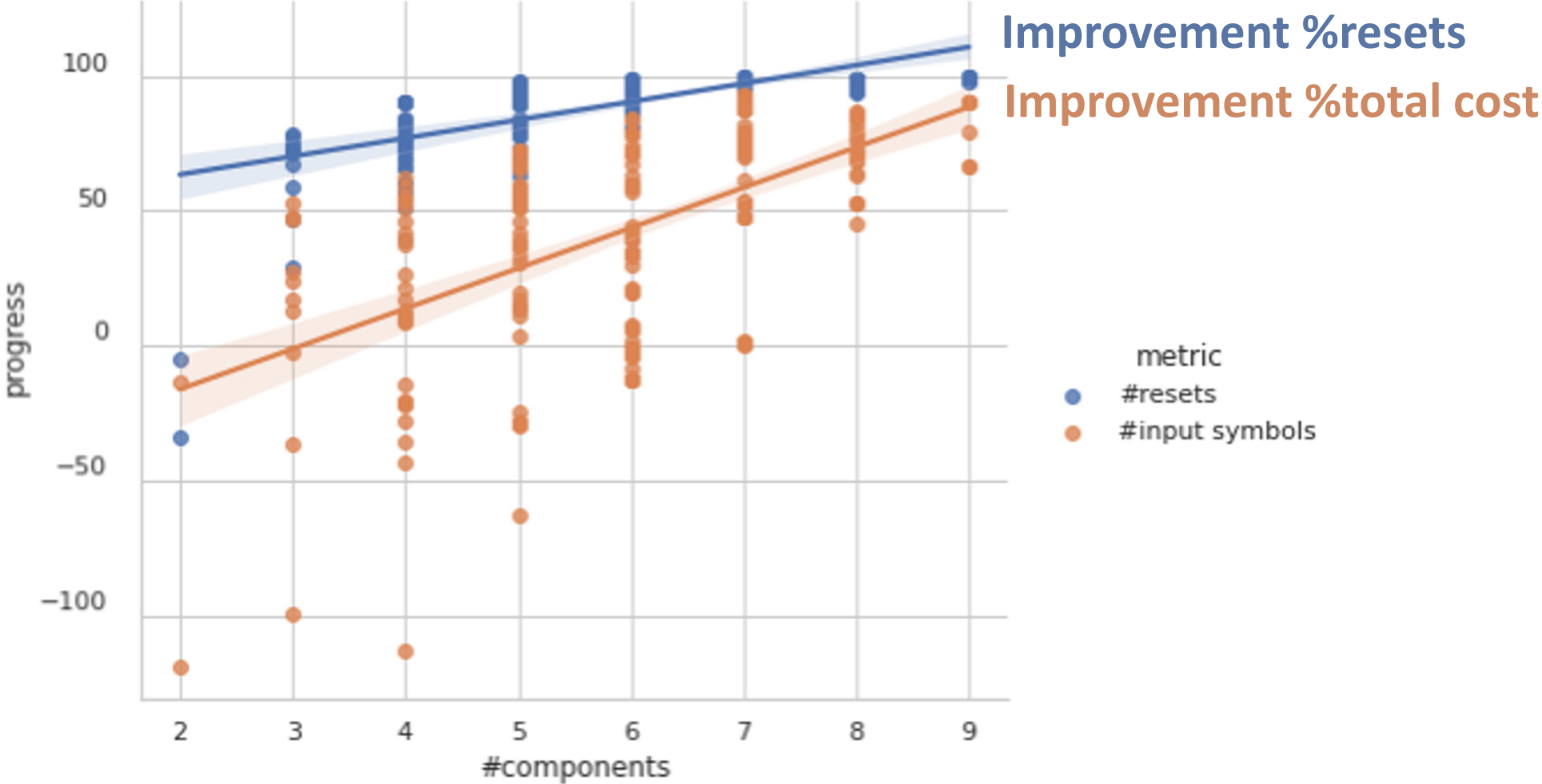
CL\* #resets L\* #resets



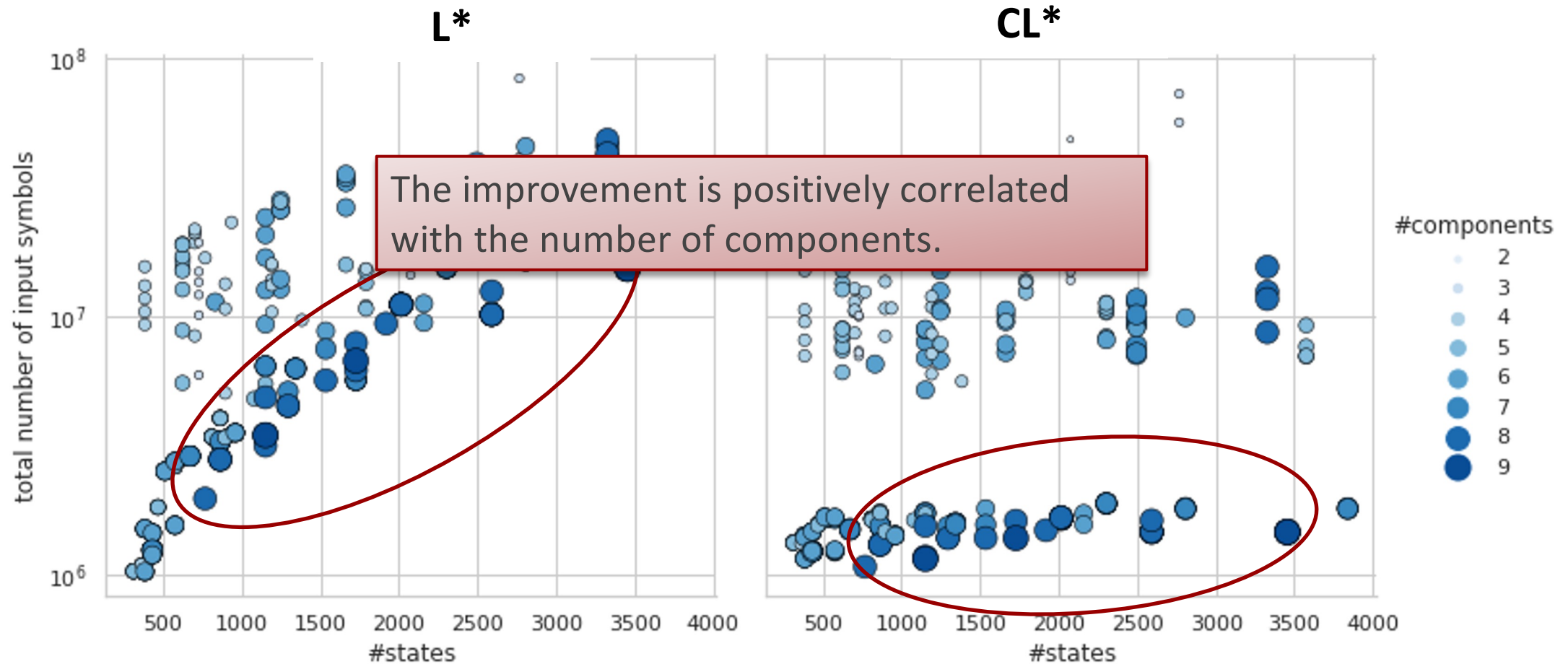
CL\* total cost L\* total cost



# Experiments: Improvement



# Experiments: Effect of Parallelism



[Labfaf, Groote, Hojjat, Mousavi, Compositional Learning for Interleaving Parallel Automata. FOSSACS 2023]



**Active Automata Learning**



**Adaptive Learning**



**Product-Line Learning**



**Compositional Learning**

# Thank you very much!

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